

# Topics

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**Buffers**

**Texture mapping**

# Buffers

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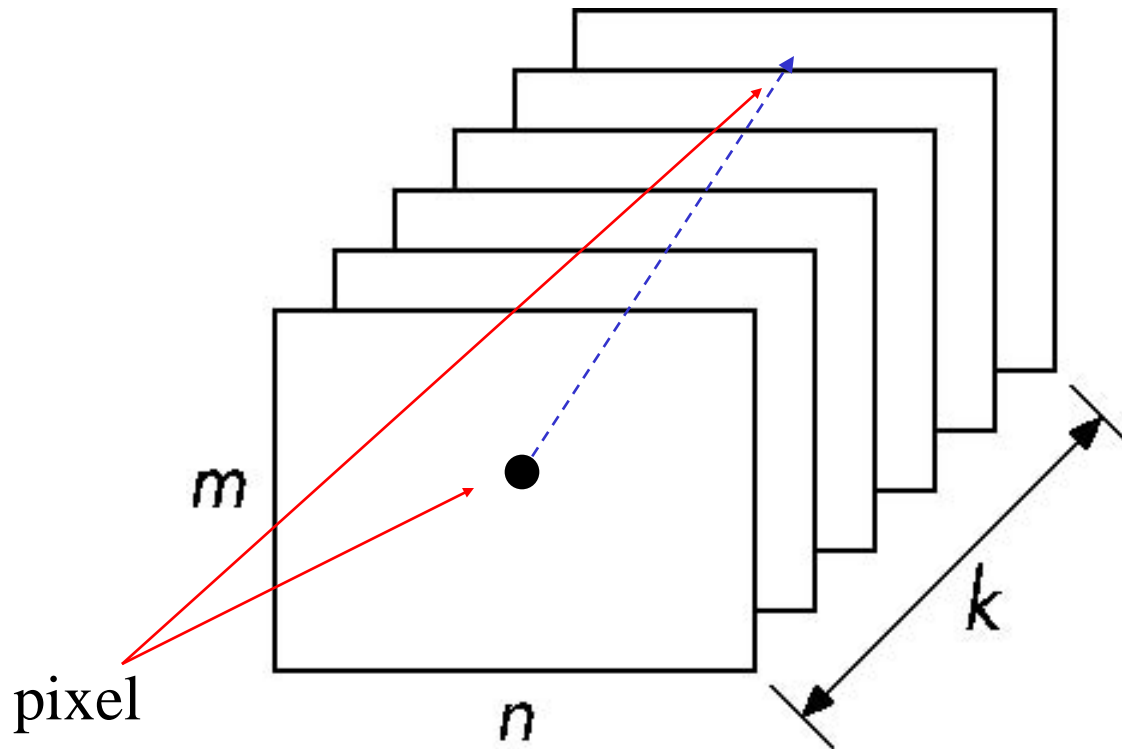
**Introduce additional OpenGL buffers**

**Learn to read from buffers**

**Learn to use blending**

# Buffer

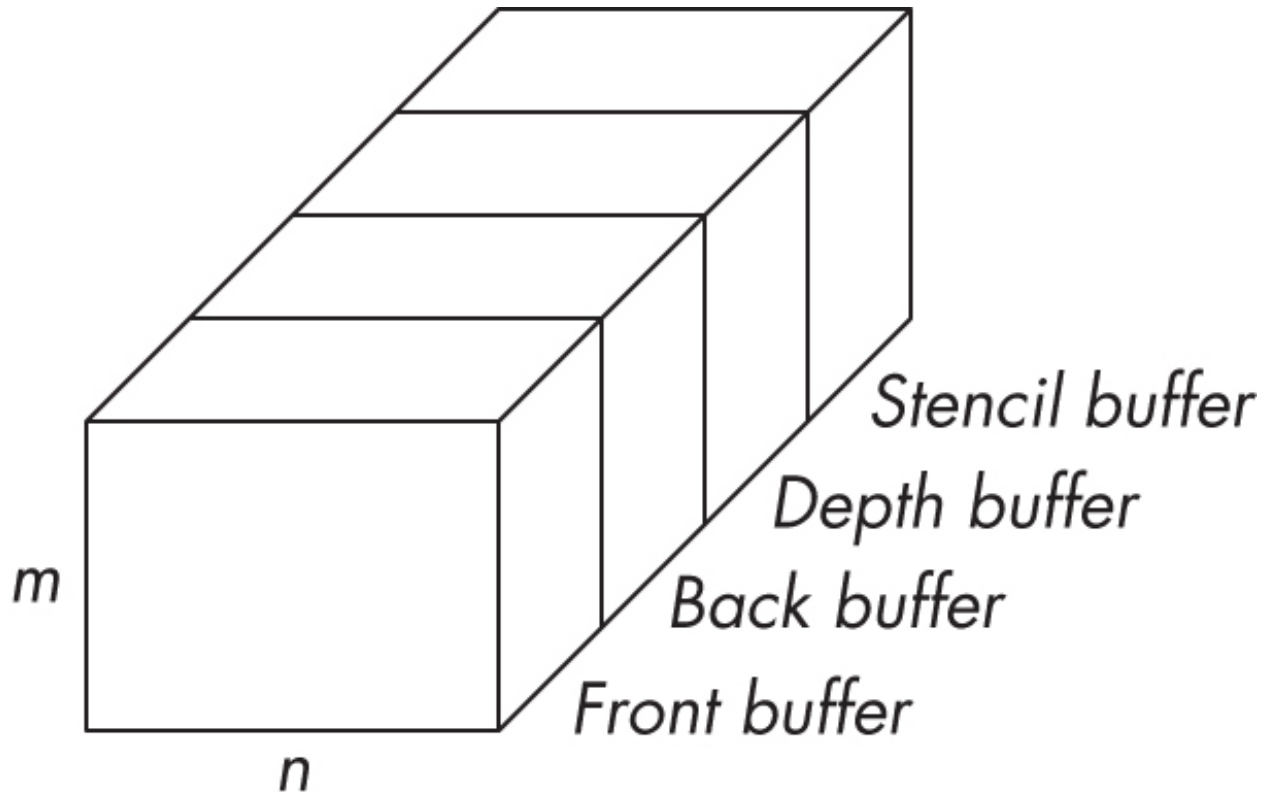
**Define a buffer by its spatial resolution ( $n \times m$ ) and its depth (or precision)  $k$ , the number of bits/pixel**



# OpenGL Frame Buffer

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**64 bits for front and back buffers**



# OpenGL Buffers

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## **Color buffers can be displayed**

- Front
- Back
- Stereo

## **Depth**

## **Stencil**

- Holds masks (per-pixel integers) to control rendering

## **Most RGBA buffers 8 bits per component**

## Writing in Buffers

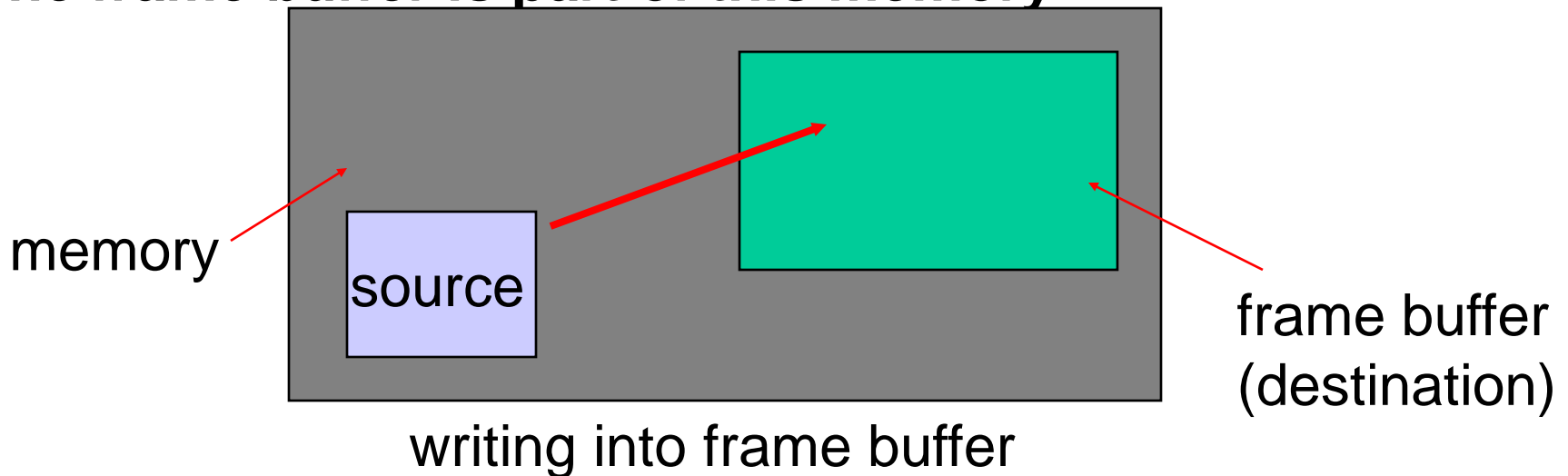
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Conceptually, we can consider all of memory as a large two-dimensional array of pixels

In practice, we read and write rectangular blocks of pixels

- *Bit block transfer (bitblt) operations*

**The frame buffer is part of this memory**



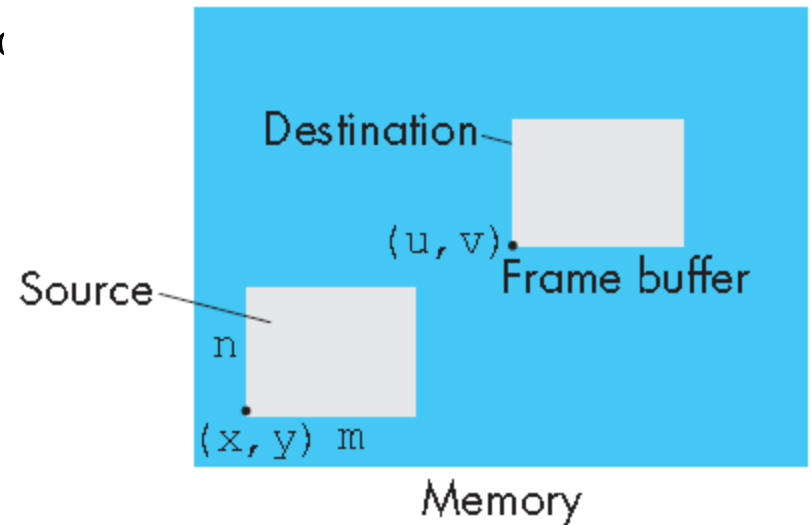
# Writing in Buffers

## Write an $n \times m$ source block with

```
write_block(source, n, m, x, y, destination, u, v);
```

Lower-left corner  
of source block

Lower-left corner of  
destination block



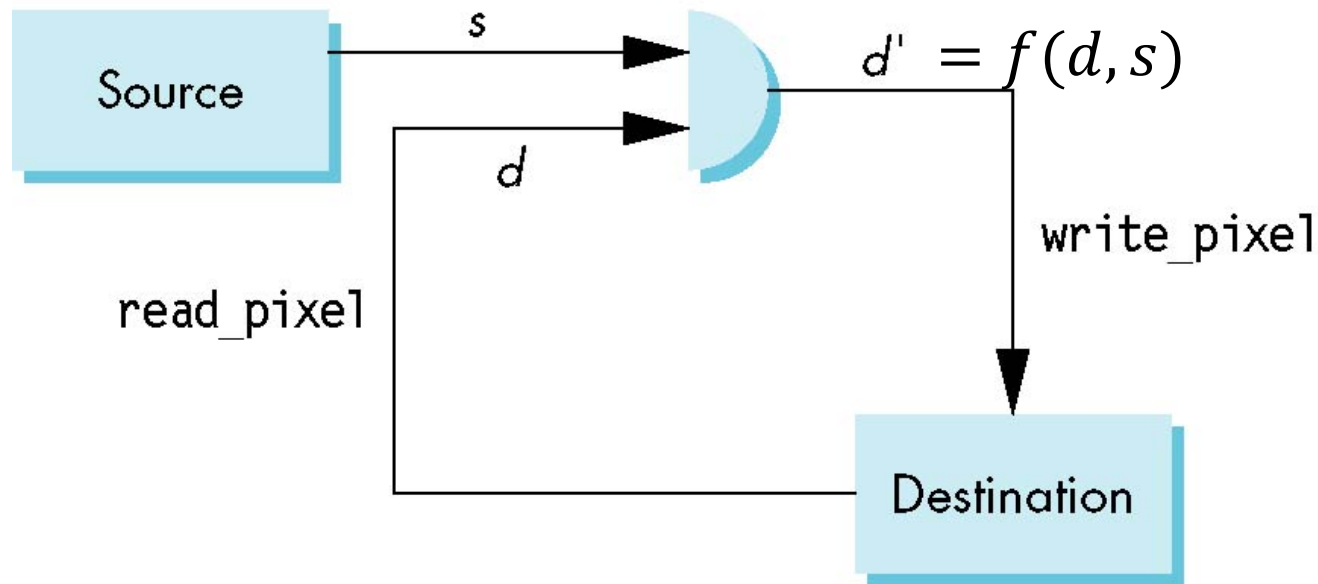
# Writing Model

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**s**: source bit

**d**: destination bit

Read destination pixel before writing source





# Bit Writing Modes

Source and destination bits are combined bitwise

16 possible functions (one per column in table)

0 and 15: clear mode;

3 and 7: write mode

$s$	$d$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
0	1	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
1	0	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
1	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1

replace      XOR    OR

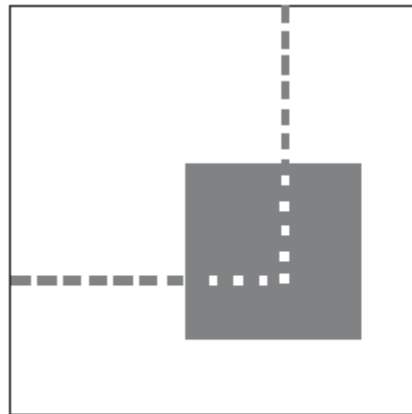
# Bit Writing Modes

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Background color: white

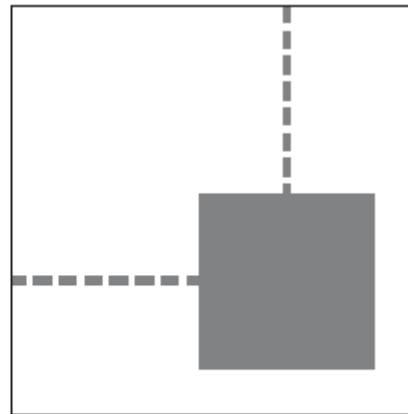
Foreground color: black

replace



Mode 3

OR



Mode 7

## XOR (Exclusive OR) Mode

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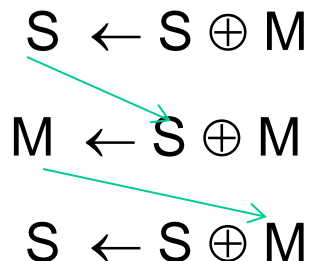
Property of XOR: return the original value if apply XOR twice

$$d = (d \oplus s) \oplus s$$

XOR is especially useful for swapping blocks of memory such as menus that are stored off screen (***backing store***)

If S represents screen and M represents a menu, the sequence

$S \leftarrow S \oplus M$   
 $M \leftarrow S \oplus M$   
 $S \leftarrow S \oplus M$



For example, S=1010, M=1100

$$S = S \oplus M = 0110$$

$$M = S \oplus M = 1010$$

$$S = S \oplus M = 1100$$

swaps S and M

# Buffer Selection

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OpenGL can read from any of the buffers (front, back, depth)

Default to the back buffer

Change with `glReadBuffer`

Drawing through texture functions

# Limits of Geometric Modeling

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Although graphics cards can render over 10 million polygons per second, that number is insufficient for many phenomena

- Clouds
- Grass
- Terrain
- Skin

# Mapping

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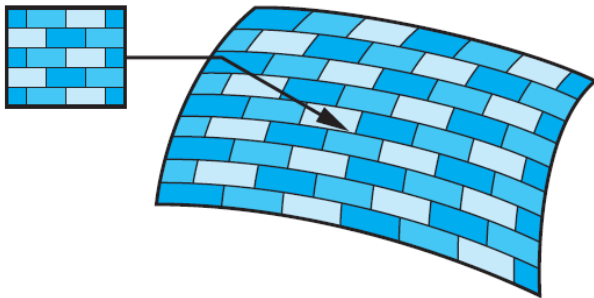
## Modify color in fragment processing after rasterization

### Three Major Mapping Methods

- **Texture Mapping**
  - Uses images to fill inside of polygons
- **Environment (reflection mapping)**
  - Uses a picture of the environment for texture maps of reflection surface
  - Allows simulation of highly specular surfaces
- **Bump mapping**
  - Emulates altering normal vectors during the rendering process

# Examples of Mapping

## Texture mapping



E. Angel and D. Shreiner: Interactive Computer Graphics 6E © Addison-Wesley 2012

## Reflection mapping



[https://en.wikipedia.org/wiki/Reflection\\_mapping](https://en.wikipedia.org/wiki/Reflection_mapping)

## Bump mapping



<http://memim.com/bumpmapping.html>

# Examples of Mapping

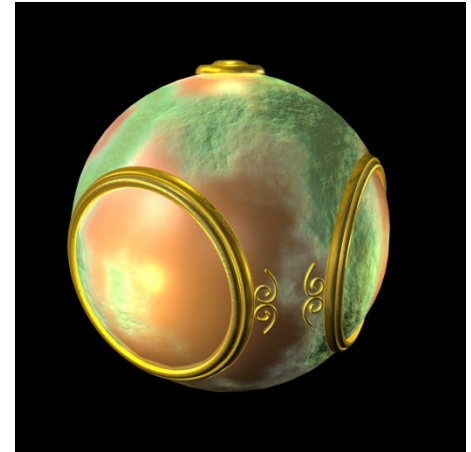
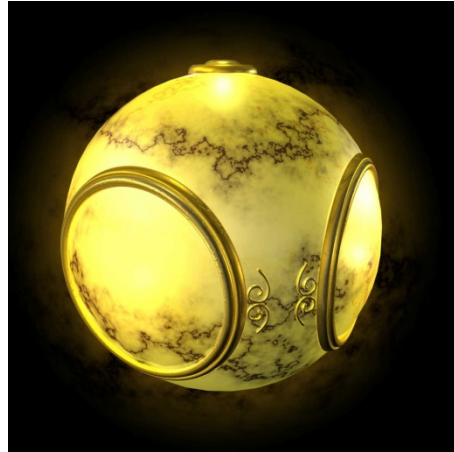
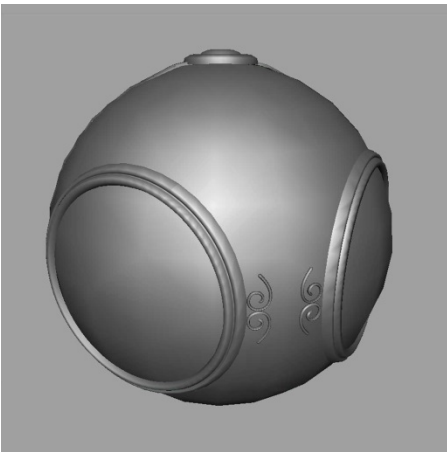
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Geometric model

Texture mapping

Reflection mapping

Bump mapping





## Modeling an Orange

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**Consider the problem of modeling an orange (the fruit)**

**Start with an orange-colored sphere**

- Too simple

**Replace sphere with a more complex shape**

- Does not capture surface characteristics (small dimples)
- Takes too many polygons to model all the dimples

## Modeling an Orange (2)

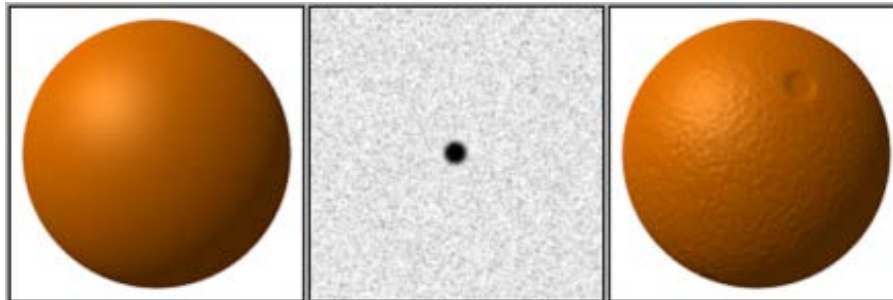
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**Take a picture of a real orange, scan it, and “paste” onto simple geometric model**

- This process is known as texture mapping

**Still might not be sufficient because resulting surface will be smooth**

- Need to change local shape
- Bump mapping

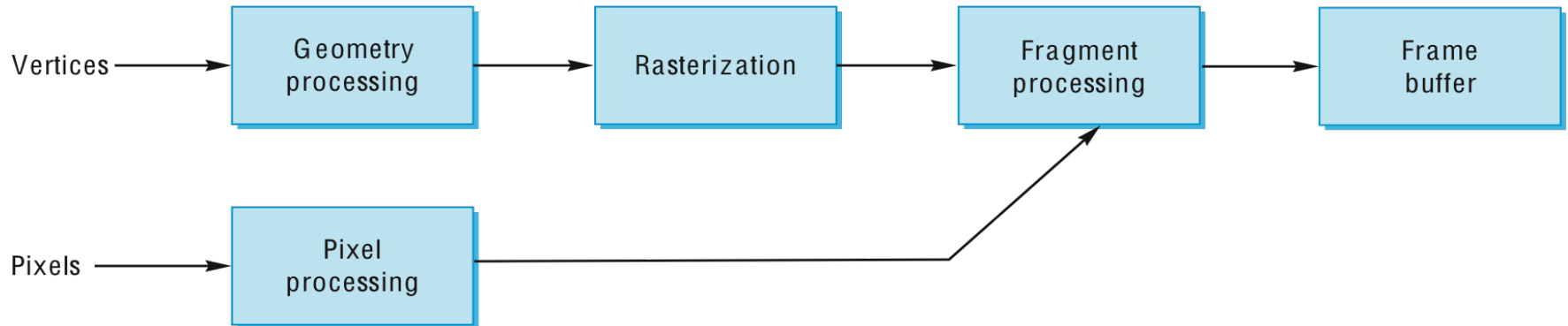


# Where does mapping take place?

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## Mapping techniques are implemented at the end of the rendering pipeline

- Very efficient because few polygons make it past the clipper



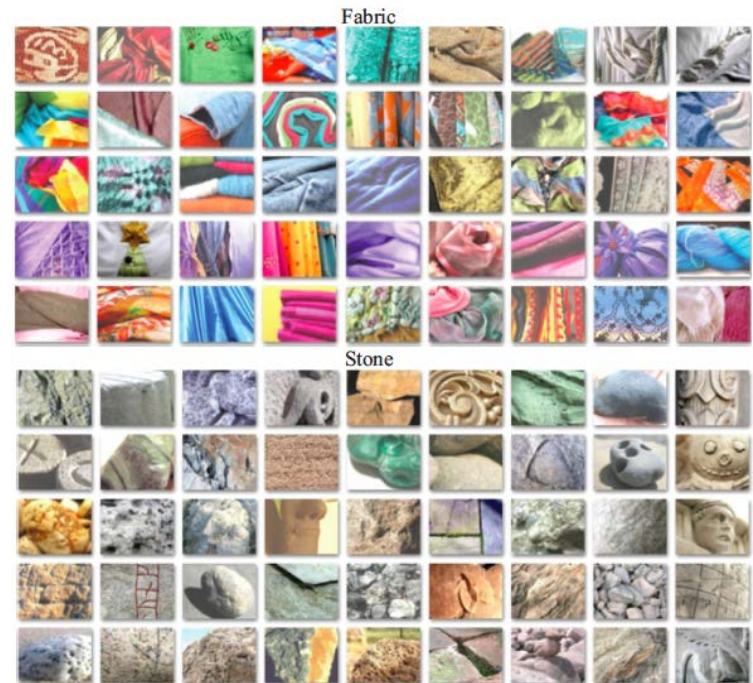
# Texture Mapping

Textures are patterns including

- Regular patterns, e.g.,
  - Stripes, checkerboards
- Complex patterns
  - Natural materials

Textures can be

- 1D – coloring a curve
- 2D – coloring surfaces
- 3D – coloring a solid block
- 4D – space-time texture



Forsyth and Ponce, “Computer Vision – A Modern Approach 2e”

Images are from Flickr Material Database,  
<https://people.csail.mit.edu/lavanya/fmd.html>

# Texture Mapping

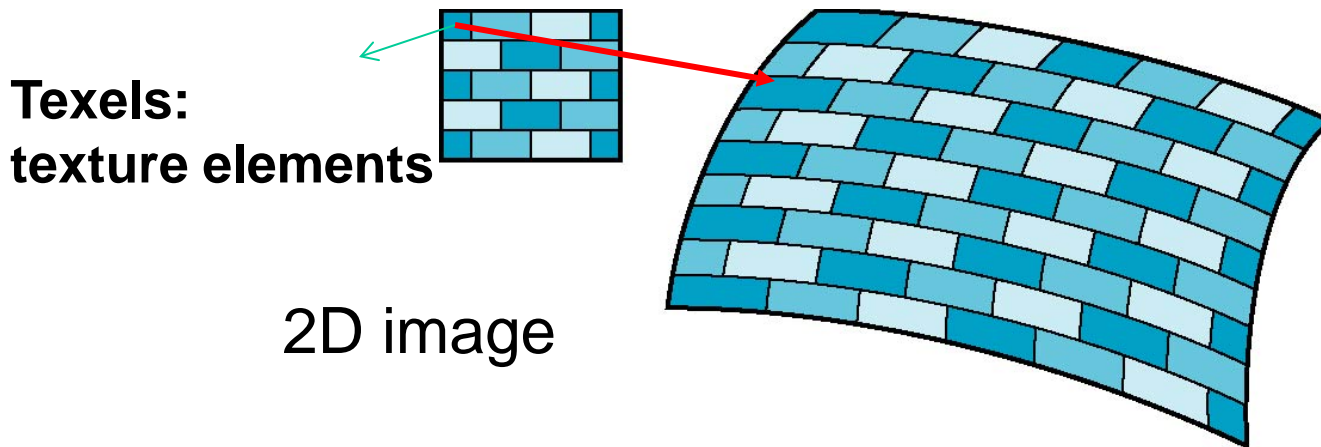
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Textures are stored in images - 2D arrays.

Each element is called a ***texel***

The idea is simple---map an image to a surface or map every texel to a point on a geometric object

However, there are 3 or 4 coordinate systems involved



# Coordinate Systems

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## **Parametric coordinates**

- May be used to model curves and curved surfaces

## **Texture coordinates**

- Used to identify points in the image to be mapped

## **Object or World Coordinates**

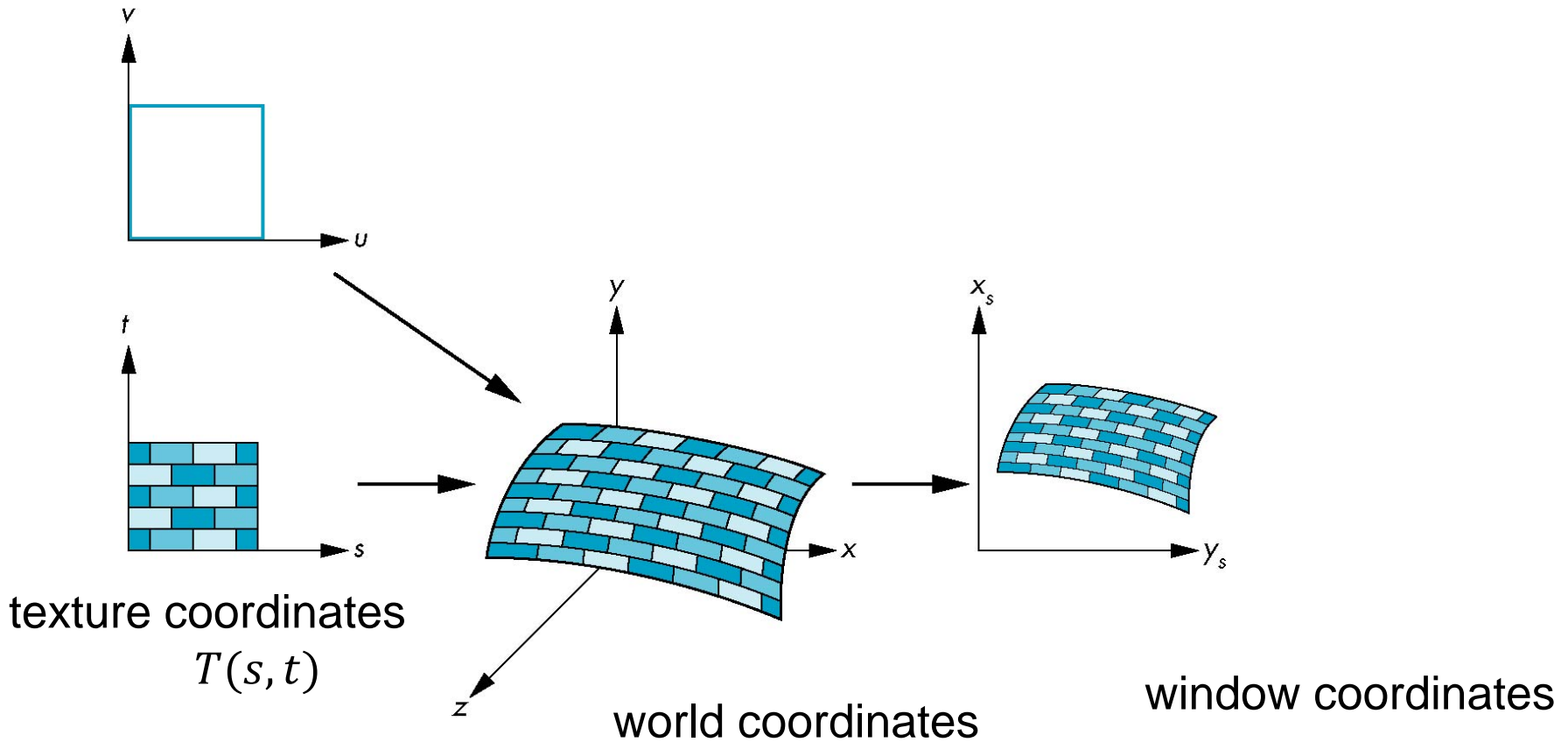
- Conceptually, where the mapping takes place

## **Window/screen Coordinates**

- Where the final image is really produced

# Texture Mapping

## parametric coordinates



# Mapping Functions

**Intuitively, consider mapping from texture coordinates to a point on a surface – forward mapping**

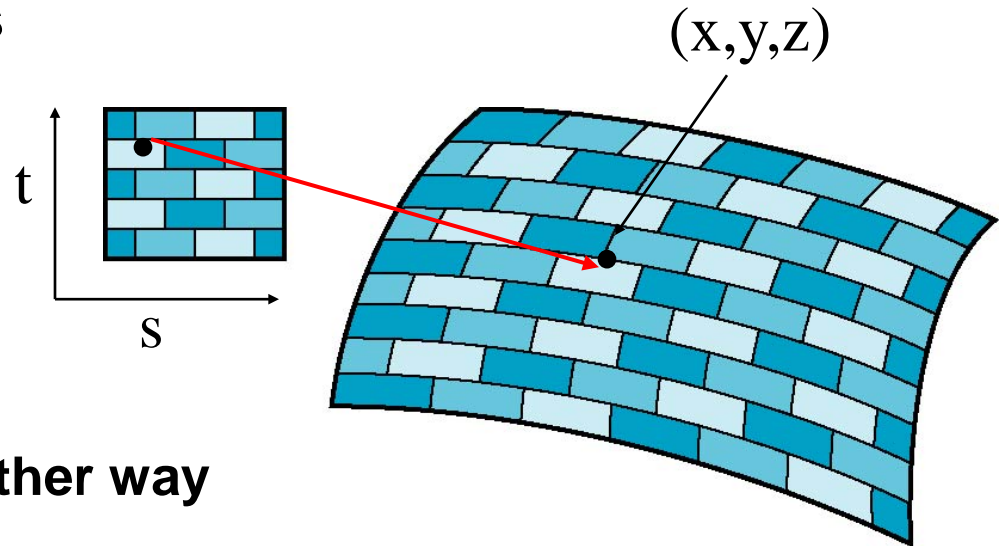
**Appear to need four functions**

$$x = x(s,t)$$

$$y = y(s,t)$$

$$z = z(s,t)$$

$$w = w(s,t)$$



**But we really want to go the other way**

**Why?**

**One severe problem- may result in holes**

E. Angel and D. Shreiner: Interactive  
Computer Graphics 6E © Addison-  
Wesley 2012



# Backward Mapping

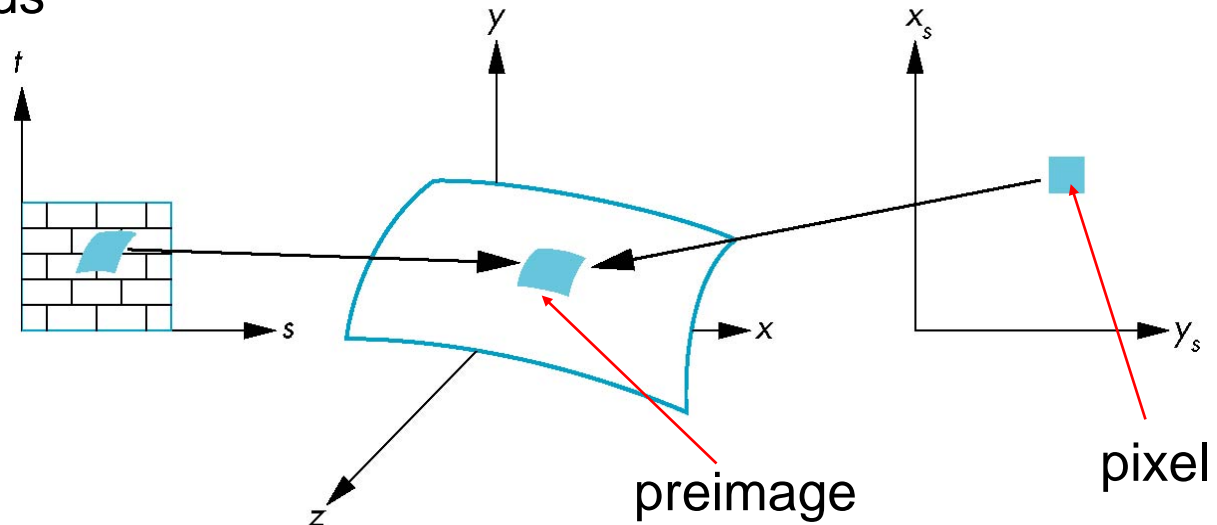
## We really want to go backwards

- Given a pixel, we want to know to which point on an object it corresponds, the preimage (inverse) of a pixel
- Given a point on an object, we want to know to which point in the texture it corresponds

## Backward mapping

$$s = s(x, y, z, w)$$

$$t = t(x, y, z, w)$$



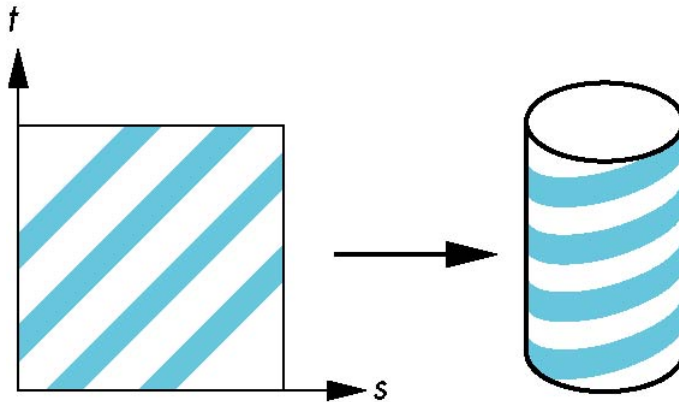
Such functions are difficult to find in general

## Two-part mapping

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One solution to the mapping problem is to first map the texture to a simple intermediate surface, e.g., a sphere, cylinder, or cube

Example: map to cylinder and then map to the target surface



# First Mapping: (1) Cylindrical Mapping

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Parametric function of a *cylinder*

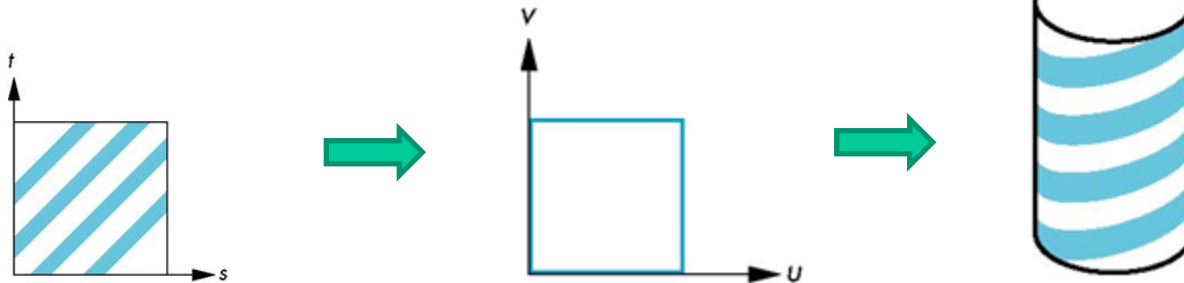
$$\begin{aligned}x &= r \cos(2\pi u) \\y &= r \sin(2\pi u) \\z &= v/h\end{aligned}$$

maps rectangle in  $u, v$  space to the curved part of a cylinder of radius  $r$  and height  $h$  in world coordinates

Parametric function of texture map

$$\begin{aligned}s &= u \quad \text{maps to texture space} \\t &= v\end{aligned}$$

The shape is not distorted



## First Mapping: (2) Spherical Map

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We can use a parametric sphere

$$\begin{aligned}x &= r \cos 2\pi u \\y &= r \sin 2\pi u \cos 2\pi v \\z &= r \sin 2\pi u \sin 2\pi v\end{aligned}$$

in a similar manner to the cylinder but have to decide where to put the distortion, e.g., at the poles



<http://richardrosenman.com/shop/spherical-mapping-corrector/>

## Spheres are often used in environmental maps

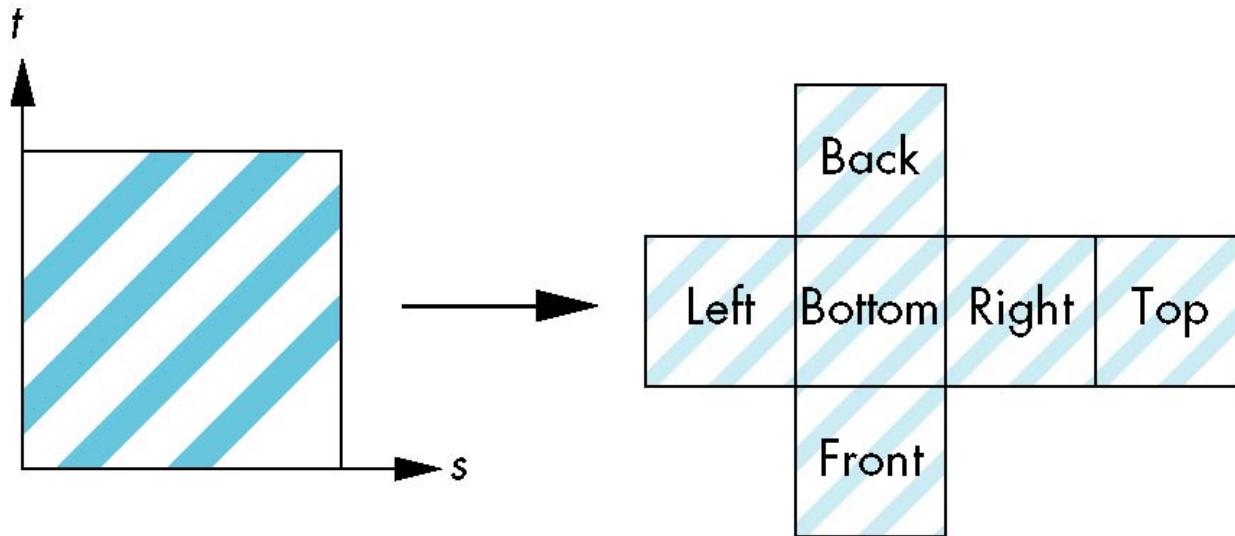
## First Mapping: (3) Box Mapping

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Map the texture to a unraveled box

Easy to use with simple orthographic projection

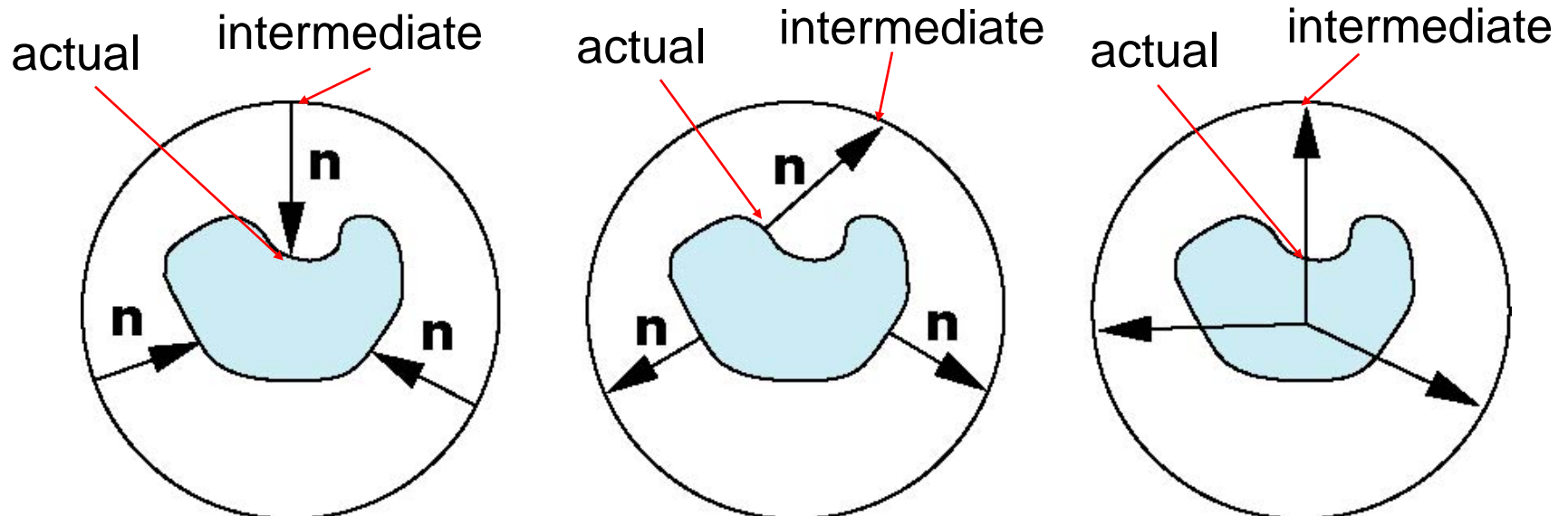
Also used in environment maps



# Second Mapping: From Intermediate Object to Actual Object

## Three strategies:

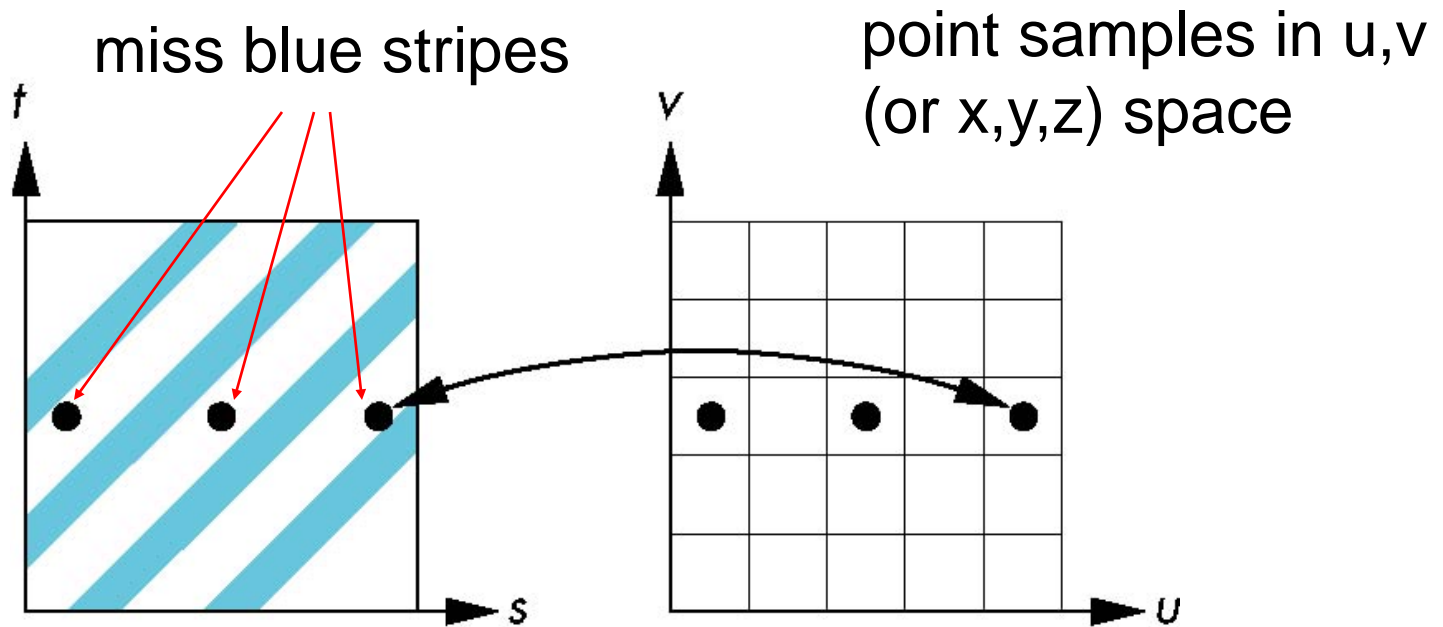
- from intermediate, along normal of intermediate until intersect with the object
- from object, along normal of the object until intersect with the intermediate
- Vectors from center of intermediate/object, intersect the object and the intermediate



# Aliasing

Backward mapping for the centers of pixels

Point sampling of the texture/object can lead to aliasing errors



## Area Averaging

A better but slower option is to use **area averaging** of the texture map over the preimage

Cannot handle high-frequency components, e.g., the stripe pattern – sampling at higher frequencies

