

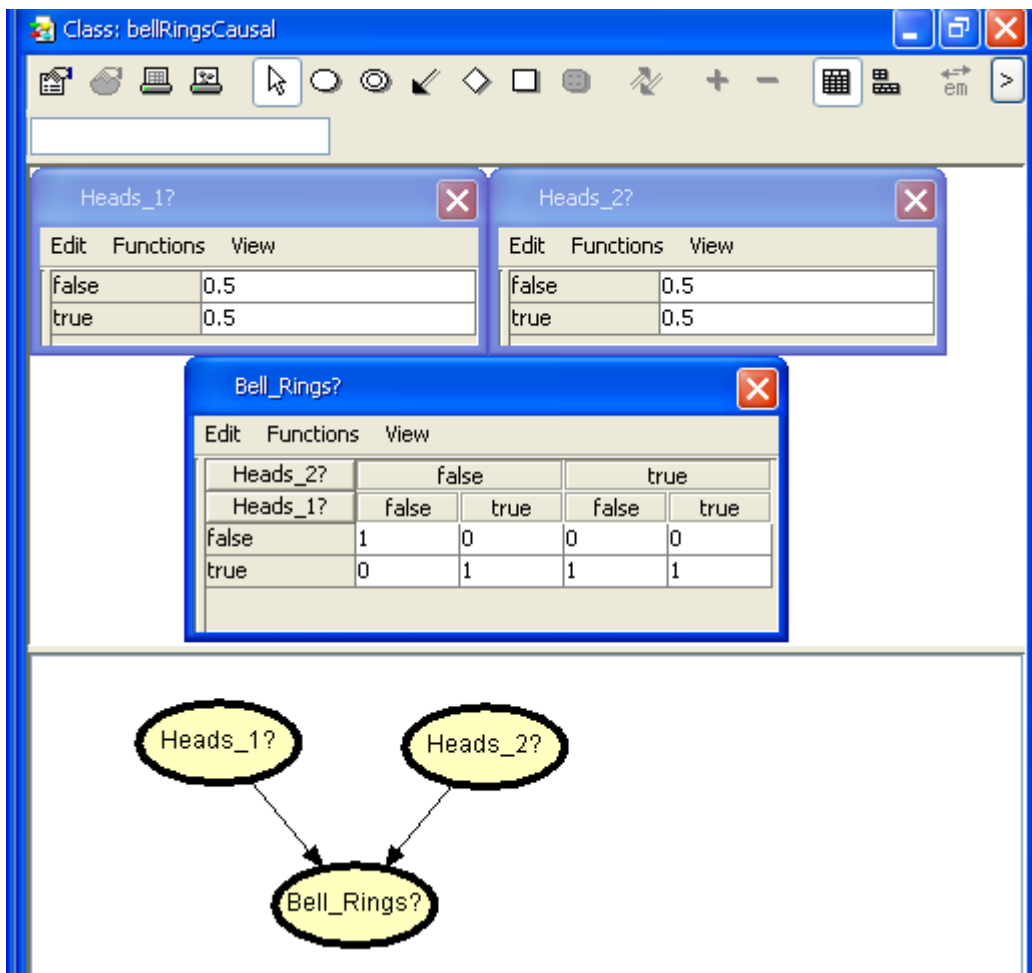
CSCE 582 Spring 2009

Test 1

2009-02-18

Closed book and notes

Consider the following simple Bayesian network. The network describes a situation in which a bell rings if and only if either one of two fair coins turns up heads.



(1—10 points) Fill the d-separation column in the table below.

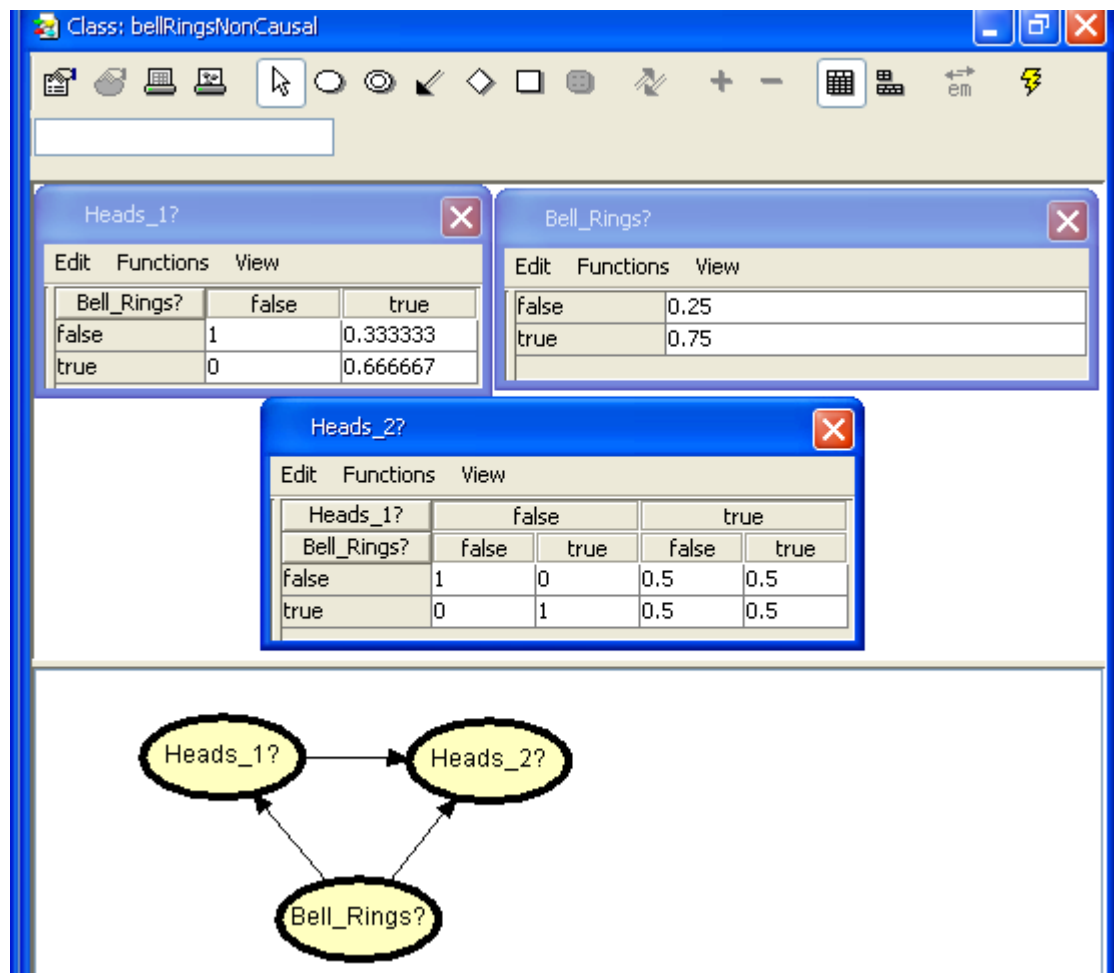
Variables	d-separated?	independent?
<i>Heads1?</i> , <i>Bell_Rings?</i>	No	No
<i>Heads2?</i> , <i>Bell_Rings?</i>	No	No
<i>Heads1?</i> , <i>Heads2?</i>	Yes	Yes
<i>Heads1?</i> , <i>Heads2?</i> given <i>Bell_Rings?</i>	No	No

(2—10 points) Compute the joint probability $P(\text{Heads1?}, \text{Heads2?}, \text{Bell_Rings?})$ by filling in the following table. The first entry is given to you.

<i>Heads1?</i>	<i>Heads2?</i>	<i>Bell_Rings?</i>	$P(\text{Heads1?}, \text{Heads2?}, \text{Bell_Rings?})$
F	F	F	$0.5 * 0.5 * 1 = 0.25$
F	F	T	$0.5 * 0.5 * 0 = 0$
F	T	F	$0.5 * 0.5 * 0 = 0$
F	T	T	$0.5 * 0.5 * 1 = 0.25$
T	F	F	$0.5 * 0.5 * 0 = 0$
T	F	T	$0.5 * 0.5 * 1 = 0.25$
T	T	F	$0.5 * 0.5 * 0 = 0$
T	T	T	$0.5 * 0.5 * 1 = 0.25$

(3—10 points) Use the table above to determine whether *Heads1?* is independent of *Heads2?* given *Bell_Rings?*. Complete the independence column in the table on the first page.

Now consider the following Bayesian network, which has the same variables as the previous one.



(4—10 points) Fill the d-separation column in the table below.

Variables	d-separated?	independent?
<i>Heads1?</i> , <i>Bell_Rings?</i>	No	No
<i>Heads2?</i> , <i>Bell_Rings?</i>	No	No
<i>Heads1?</i> , <i>Heads2?</i>	No	Yes
<i>Heads1?</i> , <i>Heads2?</i> given <i>Bell_Rings?</i>	No	No

(5—10 points) Compute the joint probability $P(\text{Heads1?}, \text{Heads2?}, \text{Bell_Rings?})$ by filling in the following table. The first entry is given to you.

<i>Heads1?</i>	<i>Heads2?</i>	<i>Bell_Rings?</i>	$P(\text{Heads1?}, \text{Heads2?}, \text{Bell_Rings?})$
F	F	F	$1*1*0.25 = 0.25$
F	F	T	$0.333*0*0.25 = 0$
F	T	F	$1*0*0.25 = 0$
F	T	T	$0.333*1*0.75 = 0.25$
T	F	F	$0*0.5*0.25 = 0$
T	F	T	$0.667*0.5*0.75 = 0.25$
T	T	F	$0*0.5*0.25 = 0$
T	T	T	$0.667*0.5*0.75 = 0.25$

(6—10 points) Use the table above to determine whether *Heads1?* is unconditionally independent of *Heads2?*. Complete the independence column in the table on the first page.

Possible answers for the first question: (1) the joint probability table above is the same as the JPT for part 2, so the same independence relations hold. (2) show that $P(\text{Heads1?}, \text{Heads2?}) = P(\text{Heads1?}) * P(\text{Heads2?})$.

(7—10 points) Here is an example from Greg Cooper via Richard Neapolitan. Suppose that metastatic cancer is a cause of brain tumor and can also cause an increase in total serum calcium. Suppose further that either a brain tumor or an increase in total serum calcium could cause a patient to fall into a coma, and that a brain tumor could cause papilledema.

Draw a causal network representing the example. Use only the following five binary variables: MetastaticCancer (present/not present), SerumCalcium (increased/not increased), BrainTumor (present/not present), Coma (present/not present), Papilledema (present/not present).

Check that in your network SerumCalcium and BrainTumor are d-separated by MetastaticCancer but are d-connected given Coma and any superset of {Coma}. Also check that BrainTumor d-separates Papilledema from the other variables.

Answer:

