## CSCE 330 Fall 2009 QUIZ 7 Assigned Wednesday, 09-10-14

with precondition  $n \ge 1$  and postcondition  $x = 2^{2^n}$ . **Answer:**  $x = 2^{2^{i-1}} \land i \le n+1$ . Also answer the following questions.

- 1. What is the precondition before the loop? Answer:  $x = 2 \land i = 1 \land n \ge 1$
- 2. Your invariant should consist of the conjuction of two formulas. One of them should be very similar to the condition of the while loop. Explain why that formula is needed. **Answer:** To insure that i = n + 1 (rather than just i > n) when the loop is exited.
- 3. Show that the precondition at the line with asterisks implies the invariant. **Answer:** In short: (1) Since i = 1 and x = 2, then  $x = 2^{2^{i-1}}$ . (2) Since i = 1 and  $n \ge 1$ , then  $i \le n+1$ .
- 4. Show that the invariant together with the negation of the loop implies the postcondition. **Answer:** In short: (1) Since  $i \le n+1$  and i > n then i = n+1. (2) Since  $x = 2^{2^{i-1}}$  and i = n+1, then  $x = 2^{2^n}$ .
- 5. Let x be the value of the variable x before executing the body of the loop and x' be the value of the variable x after executing the body of the loop. Write an equation that relates x and x'. Answer: x' = x \* x.
- 6. Let *i* be the value of the variable *i* before executing the body of the loop and *i*' be the value of the variable *i* after executing the body of the loop. Write an equation that relates *i* and *i*'. **Answer:** i' = i + 1.