

sought within a topologically open-ended space, but the fitness of a structure can often only be evaluated after parameters are assigned to key variables associated with the structures evolved. Since the structure is varied during the search process, the number of parameters and their semantics change frequently. Such problems include analog circuit design (Koza, 1999), mechanical system design (Fonseca, 1993), and neural network design (Oliker, 1992). Although a GA with a variable length representation can be used here, GP, with its outstanding capability to search simultaneously for a good structure and for appropriate parameters, distinguishes itself as the most important tool for this kind of open-ended design problem.

2.2 PREMATURE CONVERGENCE AND DIVERSITY IN THREE TYPES OF EVOLUTONARY DESIGN PROBLMES

TYPE I problems are often described as parameter optimization problems, readily addressable by GA. Premature convergence in GA has been well studied. Common diversity maintenance techniques include crowding (DeJong, 1975), deterministic crowding (Mahfoud, 1992), and fitness sharing (Goldberg, 1989). The fitness derating method (Beasley, 1993), a multi-objective method, employs fitness sharing in a popular and effective way.

The premature convergence problem when GP is applied to TYPE II problems has also been well studied. Most of the resulting methods are derived from GA, but with some specific consideration of the GP context. In multi-objective genetic programming, Rodriguez (Rodriguez-Vazquez, 1997) uses the MOGA approach with fitness sharing being performed in the fitness space, and extends it to genetic programming. Though easier to implement, it remains an open question whether diversity of fitness values is generally a true indicator of the diversity of a population – a measure which should actually be based on the parameter space. De Jong et al. (DeJong, 2001) use the multi-objective method to explicitly promote diversity by adding a diversity objective. In their method, a distance measure defined as follows is used in the diversity objective. The distance between two corresponding nodes is zero if they are identical and one if they are not. The distance between two trees is the sum of the distances of the corresponding nodes – i.e., distances between nodes that overlap when the two trees are overlaid, starting from the root. The distance between two trees is normalized by dividing by the size of the smaller of the two trees. The diversity objective is defined as the average squared distance to other members of the population. An improved version of the above distance metric between two trees is proposed by Aniko Ekart and S.Z. Nemeth (Ekart, 2000) and used to do fitness sharing in GP. Their method includes the following three steps:

- 1) The two GP trees to be compared are brought to the same tree-structure (only the contents of the nodes remain different).

- 2) The distances between each pair of symbols situated at the same position in the two trees are computed.
- 3) The distances computed in the previous step are combined in a weighted sum to form the distance of the two trees.

The major improvement of this method is that it differentiates the types of corresponding nodes when calculating the distance of two nodes. It first divides the GP functions and terminals into several subsets. For nodes whose types belong to the same subset, it calculates the relative distance. For nodes whose types belong to different subsets, it use a defined function to make sure that the distance between nodes from different subsets is bigger than that between nodes of the same subset. It also considers the fact that a difference at some node closer to the root could be more significant than a difference at some node farther from the root, using a multiplier K to distinguish them. Edit distance and phenotypic distance for fitness sharing for GP are also tested in their experiment. The former gets slightly better accuracy but with relatively high computational cost. The latter doesn't provide much improvement over the original GP without fitness sharing.

Implicit fitness sharing (McKay, 2001) has also been applied to GP. Instead of calculating the distance between the structures of GP trees, it is a kind of phenotypic (behavior-based) fitness sharing method. The fitness is "shared" based on the number of other individuals who have similar behaviors, capabilities or functions. Implicit fitness sharing provides selection pressure for each individual to make different predictions from those by other individuals. Population diversity of TYPE III problems in GP has not been investigated thoroughly. These problems are characterized by the need for simultaneous optimization of topology and parameters. In a GP population, structure diversity is needed to enable efficient topology exploration, which is the main objective, in most case, for discovery of innovative designs. At the same time, the goodness (or fitness) of a structure can only be evaluated with sufficient parameter exploration within the same structure. Thus, the parameter diversity of each structure also needs to be maintained. As a result, in the context of variable structure and parameter design by GP, the population diversity has some significant differences from that of a GA, in the following respects:

- Number of peaks

When applying fitness sharing in GA, two assumptions are made. One is that the number of peaks is known or can be estimated. Second is that the peaks are almost evenly distributed. In many problems of GA, a relatively limited number of peaks are expected to enable efficient use of fitness sharing. However, in TYPE III problems, each structure may have a huge number of peaks with respect to its parameter space, while in the structure space, each structure is a distinct peak, since the structure space is not a continuous space, but rather a highly nonlinear discrete space.

- Continuity of search space

In GA, many problems can be considered as defined in an approximately continuous space, although sometimes certain aspects have distinctly discrete behavior. However, in TYPE III problems, GP deals with a highly discrete structure space that also has a huge continuous space (of parameter values), since for each structure, the search for appropriate parameters can be regarded as an instance of GA search.

- Constraints

In GA, only parameter constraints exist. However, in TYPE III problems, GP must deal with both structure constraints and parameter constraints.

The demand for structure diversity as well as parameter diversity makes the existing fitness sharing methods inefficient for Type III problems. For fitness-space-based fitness sharing (Rodriguez-Vazquez, 1997) and the implicit fitness sharing (McKay, 2000) methods, significant parameter diversity is lost since they do not promote coexistence of individuals with the same structure but with different parameters in order to enable efficient parameter search. Fitness sharing with the distance metric, as in (Ecart, 2000; KeJong, 2001), is also inefficient in this case. First, the computational cost is still demanding, since in TYPE III problems, a complex structure and its parameters often require a big tree – perhaps 1000 - 2000 nodes in most of our experiments – especially when parameters are normally represented by a numeric subtree such as Koza uses (Koza, 1999). Second, but more importantly, the underlying assumption of the above distance metrics is that structural dissimilarity measured between two GP trees meaningfully reflects the dissimilarity in function between the two structures. However, as the structure space represented by a GP tree is a highly non-linear space, in most cases, a change of a single (non-parameter) node changes the behavior of the GP tree dramatically. This phenomenon can be traced to the weak causality of GP (Rosca, 1995), which means that small alterations in the underlying structure of a GP tree cause big changes in the behavior of the GP tree. So measuring a sort of "Hamming" distance between the structures of two GP trees to predict the difference of the behavior/function is not well founded, and thus inefficient. This makes a useful definition of a sharing radius hard to determine. It seems that distance metrics in the structure space and the parameter space and the association of a set of parameters with the structure to which they apply must be faithfully captured in order to most effectively maintain both structure diversity and parameter diversity and thereby to achieve efficient search. Therefore, given the inherent difficulty of structure/function mapping, perhaps it is counterproductive to use any structural similarity measure beyond the most basic and completely faithful one – the identity mapping: two structures are either identical, or they are not. That is the structural distance measure used here. While it is possible to define a broader relationship that still captures identity of function (for example, if swapping of the order of two children of a node has no effect on the function computed),

such definitions depend on the semantics of the functions, and were not implemented here.

3 BALANCED STRUCTURE AND PARAMETER SEARCH IN EVOLUTIONARY DESIGN BY GP

In design problems involving both variable structure and variable parameters, search must be balanced between the structure and parameters. On one hand, each structure needs sufficient exploration of its parameters to develop its potential to some extent, which means that a reasonable number of individuals of the same structure must probably be kept in the population. On the other hand, no structure should dominate the population, or it would prevent sufficient future exploration of the structure space.

Structure premature convergence in evolutionary design by GP is caused by negligence of the different role of structure and parameter search. In standard GP, crossover nodes and mutations nodes are selected randomly in the whole node set, structure operation nodes are then taken the same as the numerical nodes, (provided that numerical subtree are used to define the parameters of components, which is a standard way). This means that a circuit structure is often discarded by selection process if its fitness is low. The result is that usually, mundane structures with slightly better parameters often proliferate and dominate the population while good structure with bad parameters are discarded, which is called the structure premature problem. This phenomenon arises from the fact that promising good structures are often discarded just because its parameters are not adjusted well enough to demonstrate their potential. Ideally, a structure should be discarded only when it is demonstrated to be bad by adjusting its parameters well enough. In addition, since there is often much more numeric nodes than structure operating nodes, structure premature problem is even more severe, since there is few chance for a structure node to be selected to change the structure.

In order to solve this problem, structure and parameter search must be controlled explicitly. In our work, a probabilistic method is firstly devised to decide whether GP does a structure operation (crossover or mutation on a structure operation node) or does parameter operation (crossover or mutation on a parameter operation node). Since structure changes have more fundamental effect than the parameter changes on performance of the system, the following probabilities are defined to keep the structure and its function stable and to allow parameter adjusted well enough to demonstrate the potential of structure sufficiently.

$$p(\text{structure operation}) = 0.9$$

$$p(\text{parameter operation}) = 0.1$$

We also use explicit control of the node selection process to achieve balanced parameter evolution for all parameters in a structure. During the parameter operation stage, we first establish a list for all variables whose value need to be established during evolution, and then we randomly select a variable as the current variable to be changed. We

then select a node in the numeric sub-tree of this variable and do crossover or mutation operation. In this way, each variable has equal opportunity to be changed during evolution. This improvement speeds the evolution process balanced numeric subtrees in GP trees are achieved. All variables have numeric sub-trees with similar.

Even with above methods, the structure convergence is still often as some structures with good parameters quickly dominate the whole population. So we proposed the Structure Fitness Sharing (SFS) method to control the reproduction of high-fitness structures. Our assumptions are that fitness sharing can profitably be based on the number of individuals with the same structure, and that distance between the structures of two GP trees is not generally an adequate predictor of the differences between their behaviors. Thus, any ‘‘counting of positions where the trees differ’’ distance metric is not well founded. Instead, a simple labeling technique is used to distinguish structures.

4 STRUCTURE FITNESS SHARING (SFS)

Structure Fitness Sharing is the application of fitness sharing to structures in GP. In contrast to the GA fitness sharing using a distance measure to identify peaks, in SFS, fitness sharing is based on the tree structures, treating each tree structure in GP as a peak in the space of parameters and structures.

In SFS, each structure is uniquely labeled, whenever it is first created. So long as GP operations on an individual do not change its structure, but only its parameters, the structure label of this individual is not changed. Parameter crossover and mutation, or replication of the individual, simply increase the number of individuals with this structure (label) in the population. If structure operations are conducted on an individual that change the structure – for example, we change a Rep_C to a Rep_I node – then a new structure label (structureID) is created to label this new structure and is attached to this new individual. Our assumption is that the possibility that any particular structure-altering operation produces exactly the same structure possessed by other individuals in the current population is relatively low, so it is not necessary (or worthwhile) to check a new structure against all other existing structures to see if it is identical with one of them (and so could use its label). Furthermore, even in the case that some newly created individuals share the same structure with other individuals but are labeled with different structure labels, the algorithm is not strongly affected, as this occurs infrequently.

In standard GP, individuals with certain structures will prosper while others will disappear because of their low fitness. If this process is allowed to continue without control, some good structures (usually one) tend to dominate the population and premature convergence occurs. To maintain diversity of structures, fitness sharing is applied to individuals of each structure. SFS decreases the fitness of the individual as follows: SFS penalizes only those structures having too many individuals, according to the following fitness adjustment rule used for

experiments in this paper:

N_s : Number of structures to be searched simultaneously
 N_{sp}^s : Expected number of search points (individuals) for each structure in the whole population.

$N_{Ind_i \in S_i}^{s_i}$: Number of individuals of structure s_i to which individual Ind_i belongs.

For each individual Ind_i

If $N_{Ind_i \in S_i}^{s_i} > 0.8 * N_{sp}^s$ then

$$k = \left(\frac{N_{Ind_i \in S_i}^{s_i}}{N_{sp}^s} \right)^{-\alpha} \quad \text{where } \alpha = 1.5$$

If $k > 1$ then $k = 1.0$

$$f_{adj} = f_{old} * k \quad (1)$$

With this method, each structure has a chance to do parameter search. Premature convergence of structures is limited, and we can still devote more effort to high-fitness structure search.

4.1 LABELING TECHNIQUE IN SFS

Another labeling technique is ever proposed for a genetic algorithm in (Spears, 1994), where tag bits are used for identifying different subpopulations. Spears’s result suggests that in crowding and fitness sharing of GA, we only need to decide if two individuals have the same label. The added precision of the distance metric for maintaining the diverse state of a subpopulation is often unnecessary. In SFS, the label is used only to decide if two individuals have the same label (structure) or not. We use simple integer numbers as labels rather than more complicated tag bits.

4.2 HASH TABLE TECHNIQUE IN SFS

In order to keep track of all individuals with each particular label, a hash table is used in this structure fitness sharing method -- this speeds up the access to the structure by each individual when we do crossover, mutation, and reproduction. The size of the hash table is controlled to accommodate at most 500 structures in our experiments. Each time the number of structures in the population exceeds 500, those structures in the current population with their numbers of individuals at zero or those with a low best fitness and a high age of structure (generations since label was created) are eliminated.

4.3 THE STRUCTURE FITNESS SHARING ALGORITHM IN GP

The following is the outline of the algorithm of SFS applied to GP:

Step 1: Initialize the population with randomly generated individuals. Initialize the structure hash table.

Step 2: Assign each individual a unique label. Here a label is just an unassigned integer number incremented by one at each assignment.

Step 3: Loop over generations

3.1 Select the parents for a genetic operation according to their standard fitness

3.2: If current operation is an operation that changes the structure from that of the parent(s), (including crossover and mutation at structure operator nodes of GP trees)

Create a new label for each new structure created and add the new structure item to the structure hash table.

3.3: If the current operation is a parameter operation (mutating the parameter nodes or crossing over at a parameter node) or only replication of an existing individual, do not create a new label. New individuals inherit the labels from their parents. Update information about the structure items in the hash table, including the best fitness of this structure, number of individuals, age, etc.

3.4: If the maximum number of structures in the hash table is reached, purge individuals with the structure having the lowest best fitness or longest age, replacing them with new individuals formed by crossover or mutation.

3.5: Adjust the fitness of each individual according to (1).

Step 4: If stopping criterion is satisfied, stop; else go to step 3.

5 EXPERIMENTS

5.1 PROBLEM DEFINITION

GP with the SFS technique has been applied to a real-world analog circuit synthesis problem that was previously approached using GP without SFS (Seo, 2001). In this problem, an analog circuit is represented by a bond graph model (Fan, 2001) and is composed of inductors (I), resistors (R), capacitors (C), transformers (TF), gyrators (GY), and Sources of Effort (SE). The task is to synthesize a circuit, including its topology and sizing of components, to achieve a specified behavior. In this case, the objective is to evolve an analog circuit with response properties characterized by a pre-specified set of eigenvalues. By increasing the number of eigenvalues specified, we can define a series of synthesis problems of increasing difficulty, in which premature convergence problems become more and more significant when traditional GP methods are used. This problem of eigenvalue assignment has received a great deal of attention in control system design. Control over eigenvalues in designing systems, in order to avoid

instability and to provide particular response characteristics, is often an important and practical problem.

Circuit synthesis by GP is a well-studied problem that generally demands large computational power to achieve good results. Since both the topology and the parameters of a circuit affect its performance, it is easy to get stuck in the evolution process.

5.2 EXPERIMENTAL SETUP

In the example that follows, a set of target eigenvalues is given and a bond graph model with those eigenvalues is generated. The following three sets of 6, 8, and 10 target eigenvalues were used as targets for example genetic programming runs:

TABLE 1. TARGET EIGENVALUES

Problem 1:	6-eigenvalue problem
	$-0.1? .0j, -1.0? .0j, -2.0? .0j$
Problem 2:	8-eigenvalue problem
	$-0.1? .0j, -1.0? .0j, -2.0? .0j, -3.0 \pm 0.7j$
Problem 3:	10-eigenvalue problem
	$-0.1? .0j, -1.0? .0j, -2.0? .0j, -3.0 \pm 0.7j, -4.0 \pm 0.4j$

The following sets of experiments (total 12 = 3 problems * 4 algorithms) were conducted, with each run repeated 10 times, all with different random seeds.

The embryo model used is shown in Figure 1. It represents an embryo bond graph with three initial modifiable sites. Each dotted box represents an initial modifiable site. In each case, the fixed components of the embryo are sufficient to allow definition of the system input and output, yielding a system for which the eigenvalues can be evaluated, including appropriate impedances. The construction steps specified in the GP tree are executed at that point. The numbers in parentheses represent the parameter values of the elements.

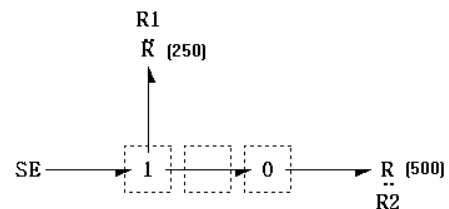


Figure 1. The Embryo Bond Graph Model

Three circuits with increasing difficulty are to be synthesized, with eigenvalue sets as specified above. Circuits were evolved with single-population GP, multiple-population GP with or without SFS. The GP parameter tableau for the single population method is

shown in Table 2 below.

First, it is important to notice that these problems exhibit a very high degree of epistasis, as a change in the placement of any pair of eigenvalues has a strong effect on the location of the remaining eigenvalues. Eigenvalue placement is very different from “one-max” or additively decomposable optimization problems, and constitutes an increasingly difficult sequence of problems with the problem order. The performance of each of the three GP approaches is reported in Figure 2, where the three GP methods are indicated by

- OneGP: single population GP
- MulGP: multi-population GP
- ONE.SFS: single population GP with SFS
- MULPOP.SFS: multi-population GP with SFS

Table 2 Parameter Settings for GP

Parameters of Single Population GP	Popsiz: 1000 init.method = half_and_half init.depth = 3-6 max_nodes = 1000 max_depth = 15 crossover rate = 0.9 mutation rate = 0.1 max_generation = 1000
Additional Parameters of Multi-Population GP	Number of subpopulations = 10; Size of subpop = 100 migration interval = 10 generations migration strategy: ring topology, migrate 10 best individuals to the next subpopulation in the ring to replace its 10 worst individuals
SFS Parameters	$N_s : 50$ $N_{sp}^s : 20 = \text{popsize} / N_s$

To observe the effect of structure fitness sharing, we monitor the number of distinct structures in the experiments with and without SFS techniques. From Fig 2, one can see that Structure Fitness Sharing can significantly improve the performance for single population GP and also does better in multi-population GP, though the difference is not as significant. The reason is that multi-population runs already provide an inherent diversity maintaining mechanism. We can also find that SFS can help probabilistic control of structure and parameter operation to maintain a stable number of search structures in the whole population.

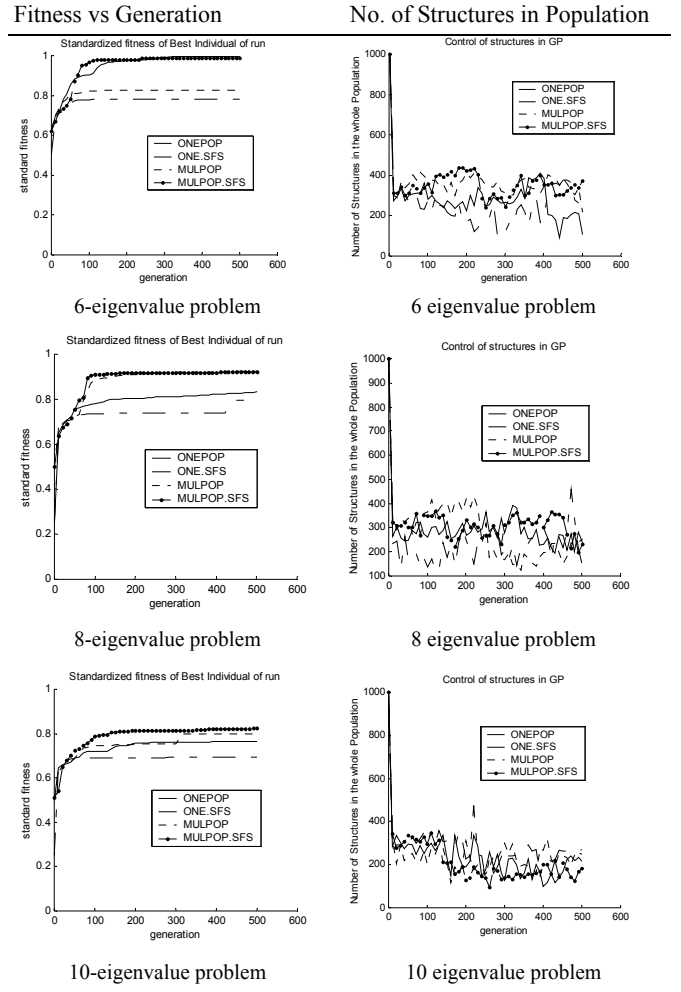


FIGURE 2. Fitness of Best Individual to Date vs. Generation & No. of Structures in Population

6 CONCLUSIONS

In this paper, Structure Fitness Sharing (SFS) is proposed to achieve balanced structure and parameter search in evolutionary design by Genetic Programming. SFS can effectively prevent the dominance of any specific structure and when combined with probabilistic control of structure and parameter operation, SFS can maintain a stable number of structures for simultaneous search. Our labeling technique in SFS eliminates the necessity of computing the distance between two individuals, which saves a lot of computing effort that is largely wasted when attempting to measure GP structural similarity. The user parameters of the standard fitness sharing method are also eliminated (e.g. the sharing radius). All that must be done is to define the fitness adjustment scheme. – that is, exactly how to penalize the fitness of a structure when the number of individuals with that structure label grows large enough to threaten the diversity of the population. The hash table technique allows SFS to quickly update the structure information about the current population during

evolution. More complicated balanced structure parameter search methods can be derived using the concept of structure diversity. For example, the authors intend to incorporate the elitist method of multi-objective evolutionary computation into SFS.

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