Instructions

Show all your steps--answers alone are not sufficient.

Homework must be done neatly.

Use straight-edged paper (no notebook tear-outs with ragged edges).

Please STAPLE papers to a signed cover sheet.

Homework Problems

Problem 5.4 (a). Plot the expression on a 4-variable K-map. (10 points)

Problem 5.4 (b). Simplify the K-map from 5.4 (a) into SOP form. Begin with a fresh map. (10 points)

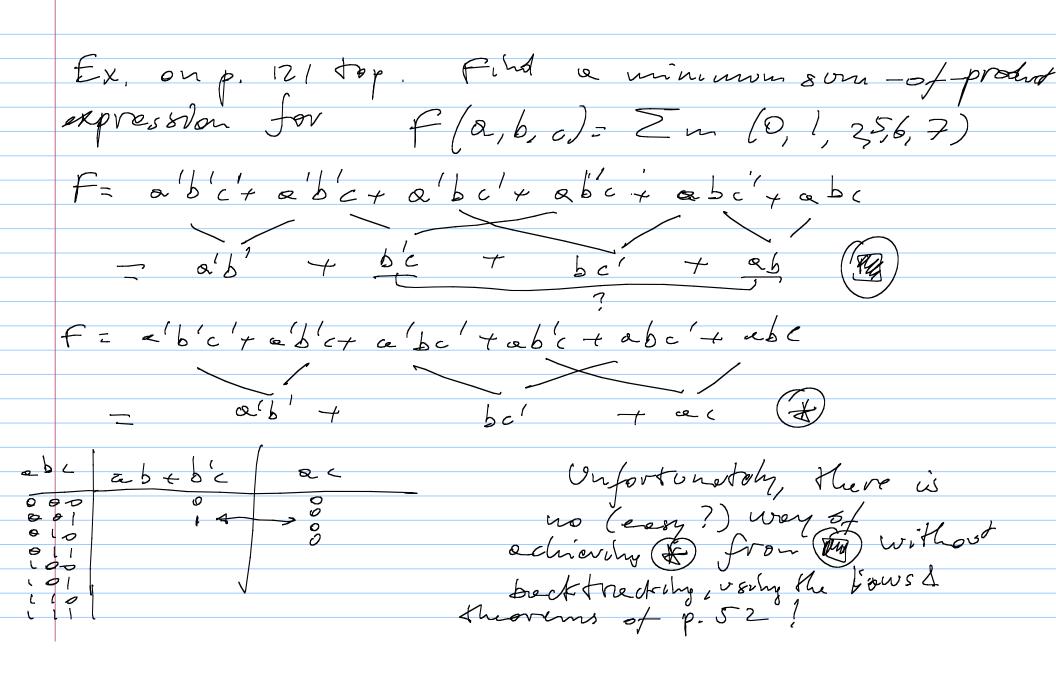
Problem 5.4 (c). Simplify the K-map from 5.4 (a) into POS form. Begin with a fresh map. (10 points)

Problem 5.6 (a). To work use guideline summary from class: gnore "essential prime implicants." (20 points

Problem 5.8 (a). (Note that the problem asks for both SOP and POS simplifications.) (20 points)

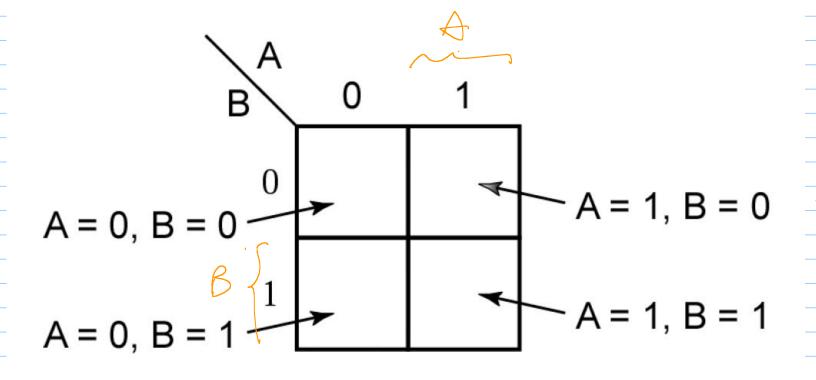
Problem 5.12 (c). (POS simplification.) (10 points)

Problem 5.21 (b). (Note that POS form is requested even though the problem statement is given in min-terms.) Plot the min-term map, then redraw with 0's, and group the 0's. (20 points)



Chapter 5

for two variables (A and B)



Section 5.2, p. 121

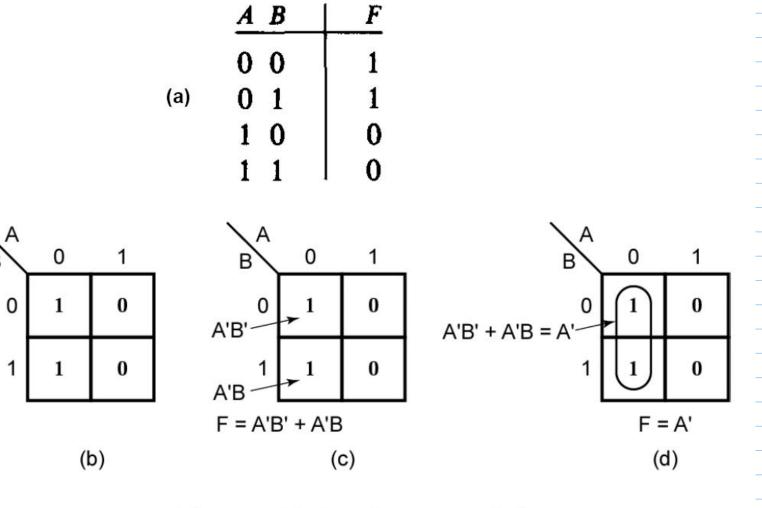


Figure 5-1a, b, c, and d

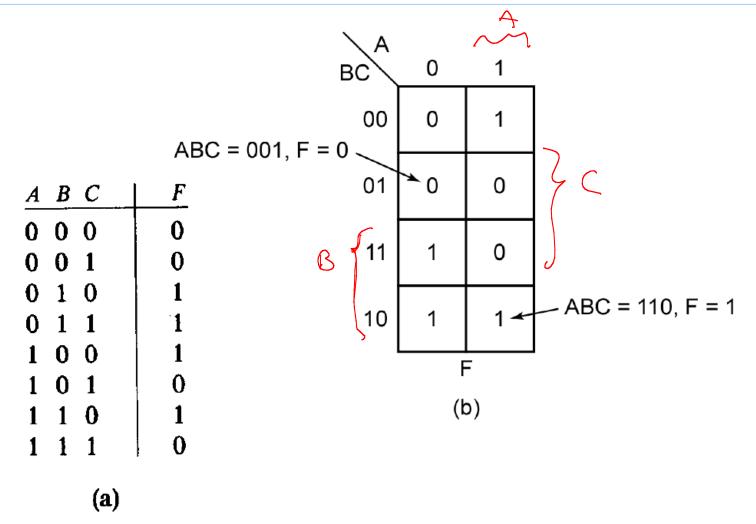


Figure 5-2: Karnaugh Map for Three-Variable Function

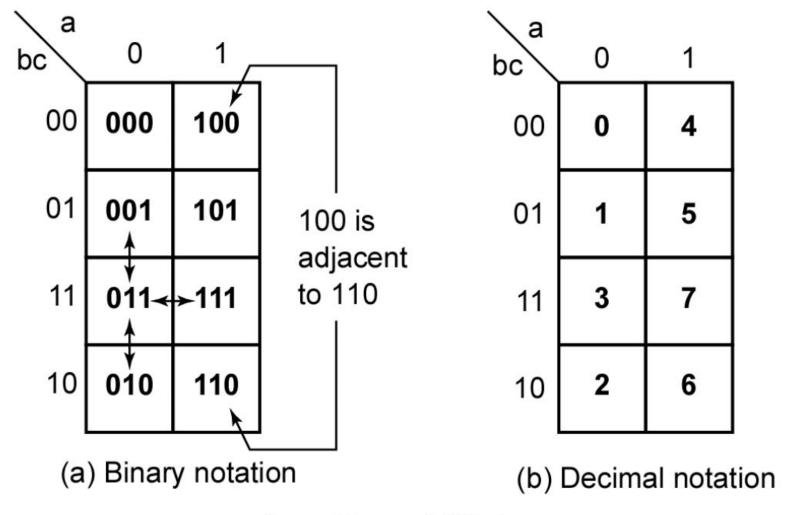


Figure 5-3: Location of Minterms on a Three-Variable Karnaugh Map

a bc	0	1
00	0 0	0 4
01	1	1 5
11	1 3	0 7
10	0 2	0 6

Figure 5-4: Karnaugh Map of $F(a, b, c) = \Sigma m(1, 3, 5) = \prod M(0, 2, 4, 6, 7)$

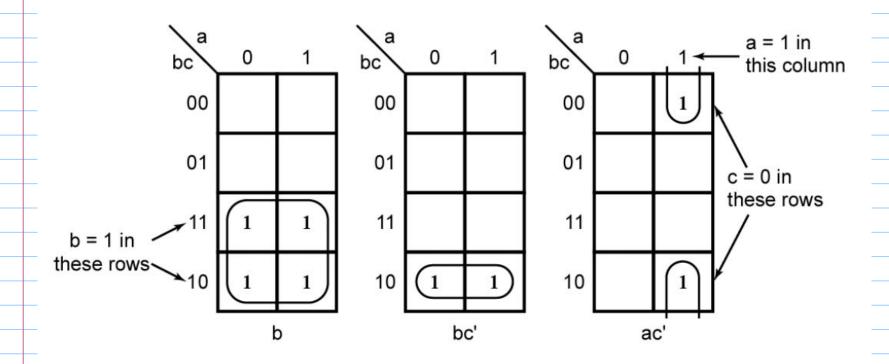
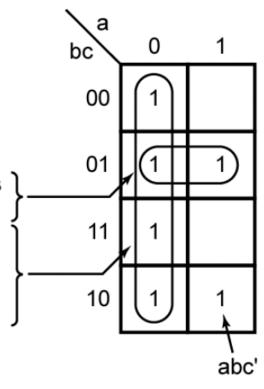


Figure 5-5: Karnaugh Maps for Product Terms

$$f(a,b,c) = abc' + b'c + a'$$

- The term abc' is 1 when a = 1 and bc = 10, so we place a 1 in the square which corresponds to the a = 1 column and the bc = 10 row of the map.
- The term b'c is 1 when bc = 01, so we place 1's in both squares of the bc = 01 row of the map.
- 3. The term a' is 1 when a = 0, so we place 1's in all the squares of the a = 0 column of the map. (Note: Since there already is a 1 in the abc = 001 square, we do not have to place a second 1 there because x + x = x.)



Section 5.2, p. 124

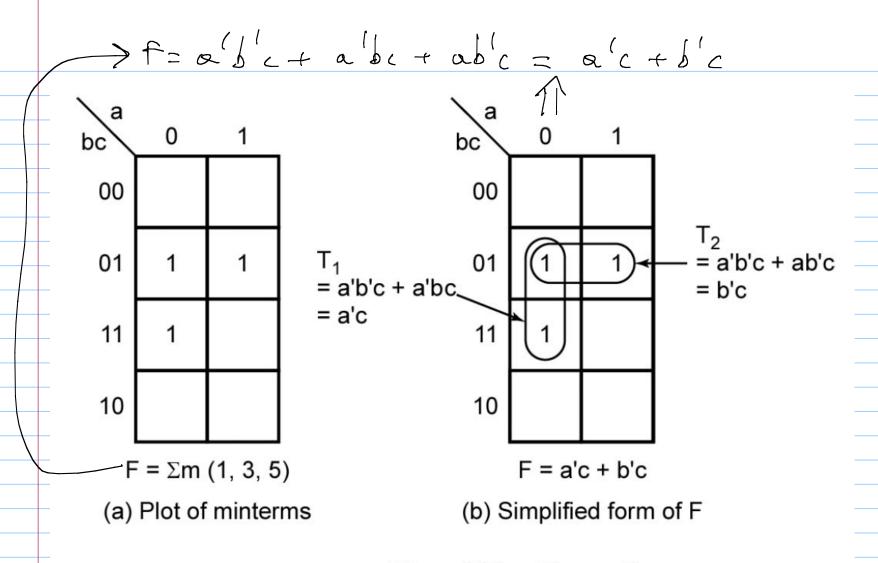


Figure 5-6: Simplification of a Three-Variable Function

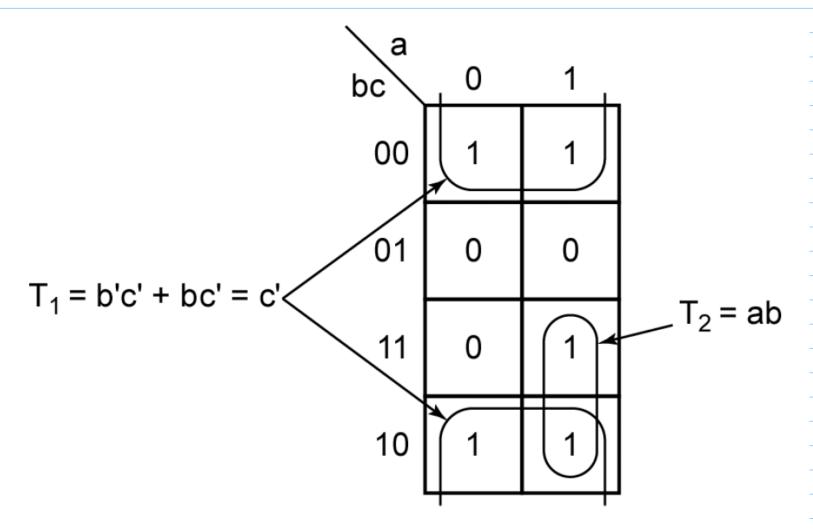


Figure 5-7: Complement of Map in Figure 5-6a

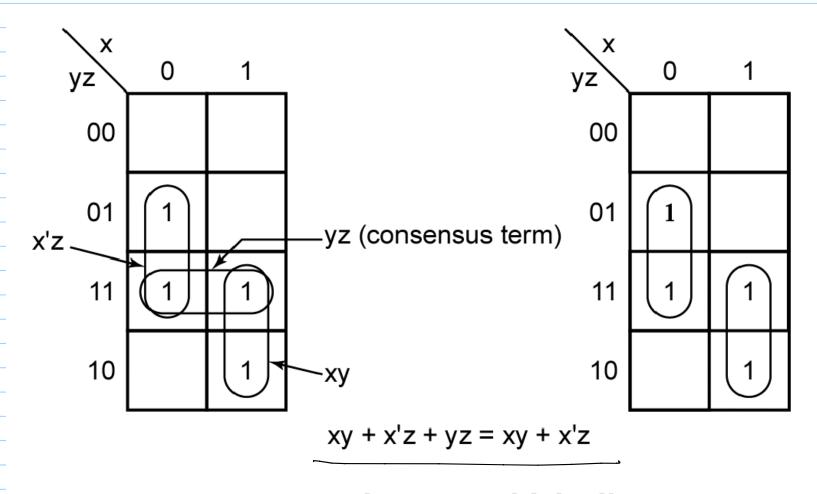


Figure 5-8: Karnaugh Maps Which Illustrate the Consensus Theorem

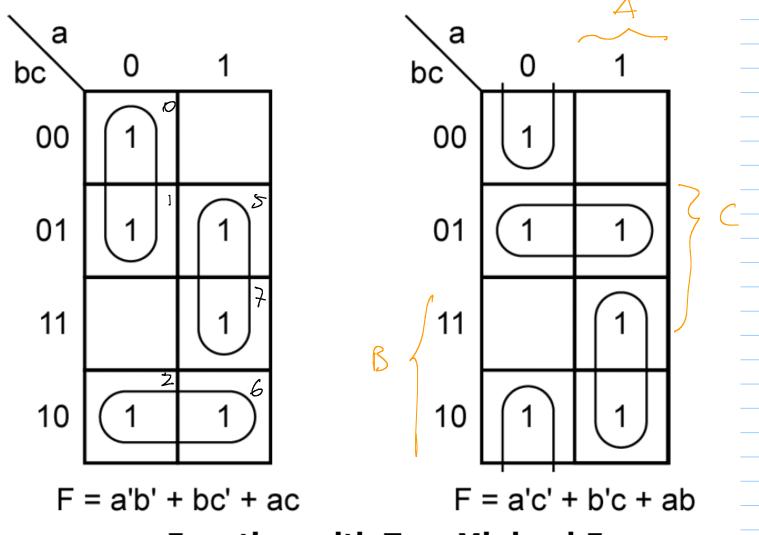
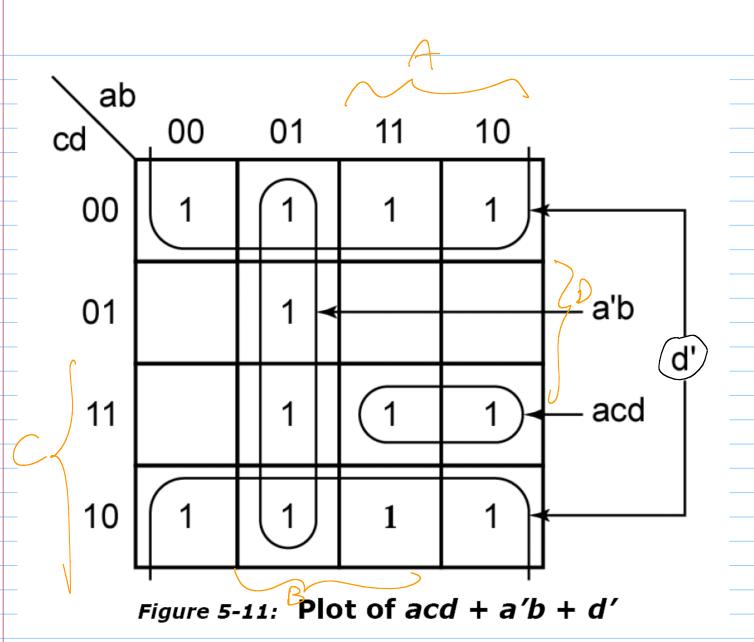
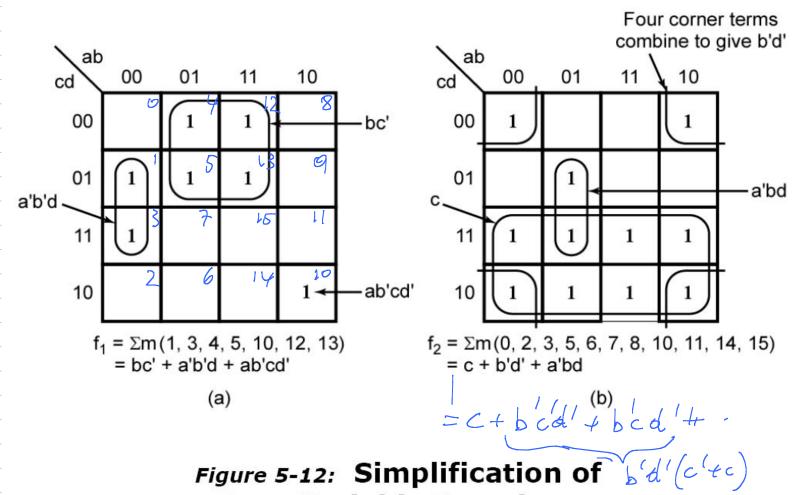


Figure 5-9: Function with Two Minimal Forms

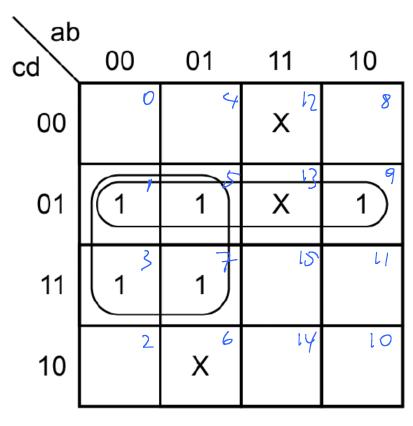
Sec	Lon	5.3	•	- 60V -	· voriable	Kornergh Maps
CD	00	01	11	10		0
00	0	4	12	8		
01	1	5	13	9		
_ ∫ 11	თ	7	15	11		
10	2	6	14	10		
			A			

Figure 5-10: Location of Minterms on Four-Variable Karnaugh Map





Four-Variable Functions



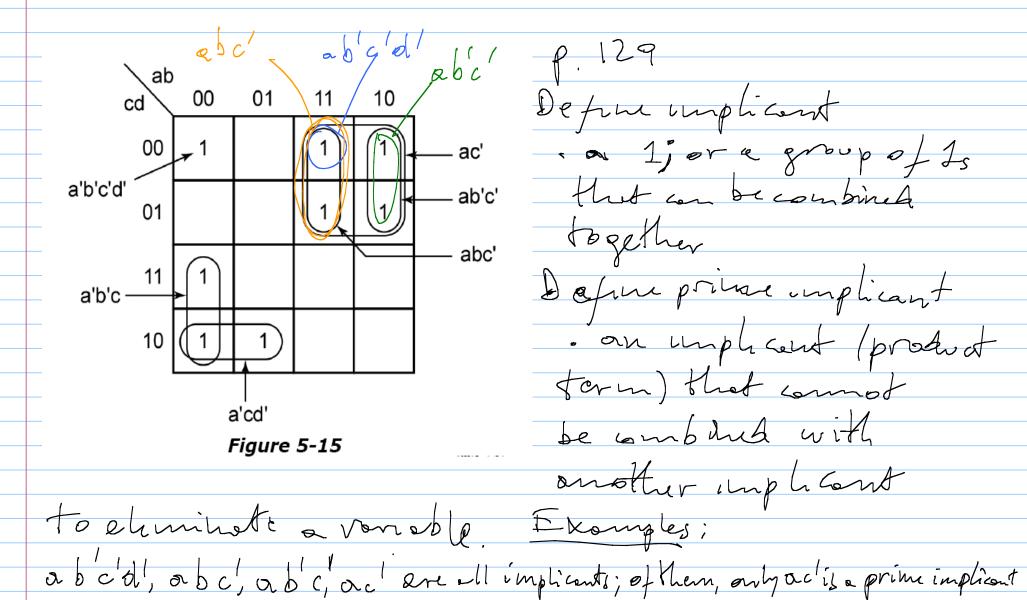
Circuit 2!

$$f = \Sigma m(1, 3, 5, 7, 9) + \Sigma d(6, 12, 13)$$

= a'd + c'd

Figure 5-13: Simplification of an Incompletely Specified Function

Find the minimum product of soms realization for J=X2 +wy2+wy8+ 00 Use the Kernery G I and sotterly = y2 +WXZ+Wxy (UX DeMorgan's law /=(Y+3). (W+X+2). (u 12/4) (a product of Joms Figure 5-14



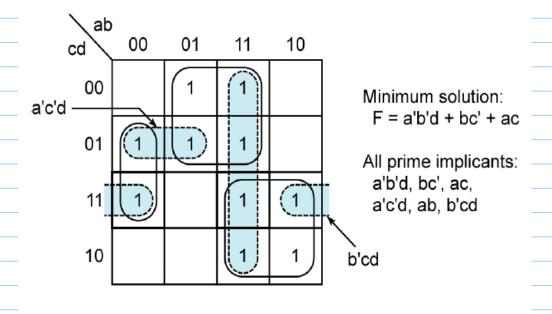
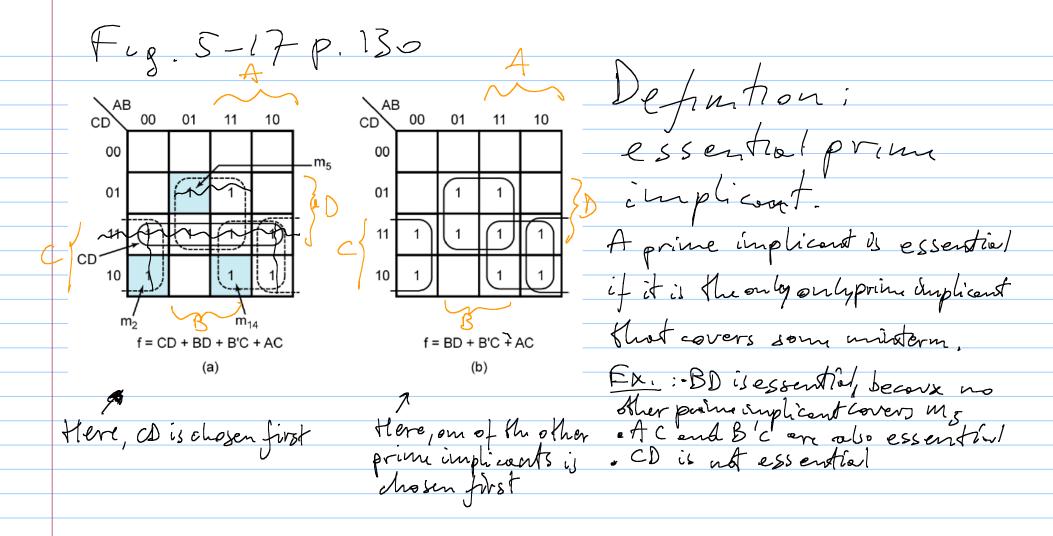
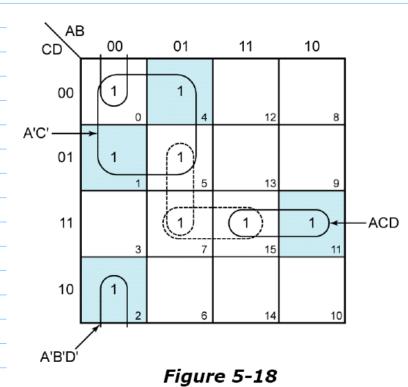


Figure 5-16: Determination of All Prime Implicants





Theorem (p. 131; p. 621)

If a given mintern and all the I's

edgicent to it are covered by a single

term, then that term is an essential

prime implicant

Example (cf. Figure 5.18);

A'C' is an essential prime implicant, because mintern 0001, (=1,0) and all the ones adjacent to it (0,4,5) are covered by A'C'.

Decause mintern 10112 (=1110) and all the one, adjacent to it (15), are covered by ACD?

· A'B'D' is an assential prime implicant, be asux mintern 10112(=2,0) one all the ones adjecent to it (0) are covered by it.

· There are no other essential prime implicants

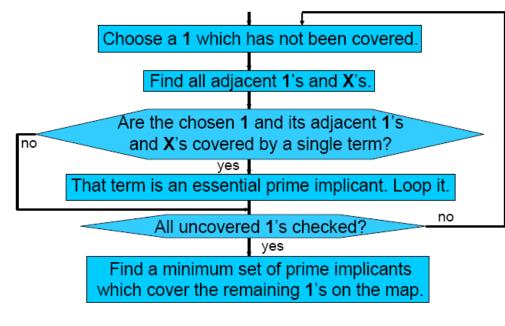


Figure 5-19:
Flowchart for Determining a Minimum Sum of Products
Using a Karnaugh Map

P.132

There are five important points to keep in mind when simplifying functions on K-maps:

- 1. Each square (minterm) on a K-map of two variables has two squares (minterms) that are logically adjacent, each square on a K-map of three variables has three adjacent squares, and so on. In general, each square on a K-map of *n* variables has *n* logically adjacent squares, with each pair of adjacent squares differing in exactly one variable.
- 2. When combining terms (squares) on a K-map we always group squares in powers of 2, that is, two squares, four squares, eight squares, and so on. Grouping two squares eliminates one variable, grouping four squares eliminates two variables, and so on. In general, grouping 2n squares eliminates n variables.
- 3. Group as many squares together as possible; the larger the group is, the fewer the number of literals in the resulting product term.
- 4. Make as few groups as possible to cover all the squares (minterms) of the function. A rninterm is *covered* if it is included in at least one group. The fewer the groups, the fewer the number of product terms in the minimized function. Each minterm may be used as many times as it is needed in steps 4 and 5; however, it must be used at least once. As soon as all minterms are used once, stop. A minterm that has been used in at least one group is said to have been *covered*.
- 5. In combining squares on the map, always begin with those squares for which there are the fewest number of adjacent squares (the "loneliest" squares on the map). Minterms with multiple adjacent minterms (called *adjacencies*) offer more possible combinations and

on the web site

F= A'B + A B'D' + AC'D. Choose ly. File its (Xo, Is, I Land & neighbors. Con you cover them withesingle 2 loop 5? 01 19 Shaded 1's are covered by (18, 15, 113, 119) only one prime implicant. 11 X_{15} Choose of It's very box of Long $\left(1_{6}\right)$ 10 We con wover 16,14,X7 with Figure 5-20 a loop, so A'BD'is en essential prime implicant. Choose In . It's neighbor is to ABD is en essentle portu implant. and In which overend by the The only ones left one 1,3 portue impligant A C'D