Ch 7 [H] Mosh futon Anelysis; "What-It for Closed Systems Preview. - osymptotic bounds - modification ome høris for absert systems.

Review (7.1[H]) Little's Lew for an Open Systems E[N] = d. E[T] (E[N]= 1. E[Ta]) (E[Nred]= A. E[Tred]) little's law for a Closed Borton System N= X. E[T]. (This actually holds for any olosed system, but for interactive abjed system, the following also holds.)

Little's law for a Closed Interactive System

E[R]= N = E[Z] (note: E[T]= N

X Utilization Low $e:=\frac{1}{1}$ = 1; $E[S_i] = X$; $E[S_i]$ Forced Flow Law

X:= E [Vi]-X

Bottleneck Low

Ci=X. E[Di], where Di is the total service demand on de vice i for all visits of a single job.

7.2 [H] Asymptotic Bounds for Closed Systems

Let on be the number of devices in the system. E[Di] is as defined before, i.e., the expected total service demand on device i by a single job let $D = \sum_{i \ge 1} E[D_i]$ Let $D = \max_{i \ge 1} f[D_i]$ Let $D = \max_{i \ge 1...m} f[D_i]$

Theorem 7.1 For any closed interactive system with N terminals,

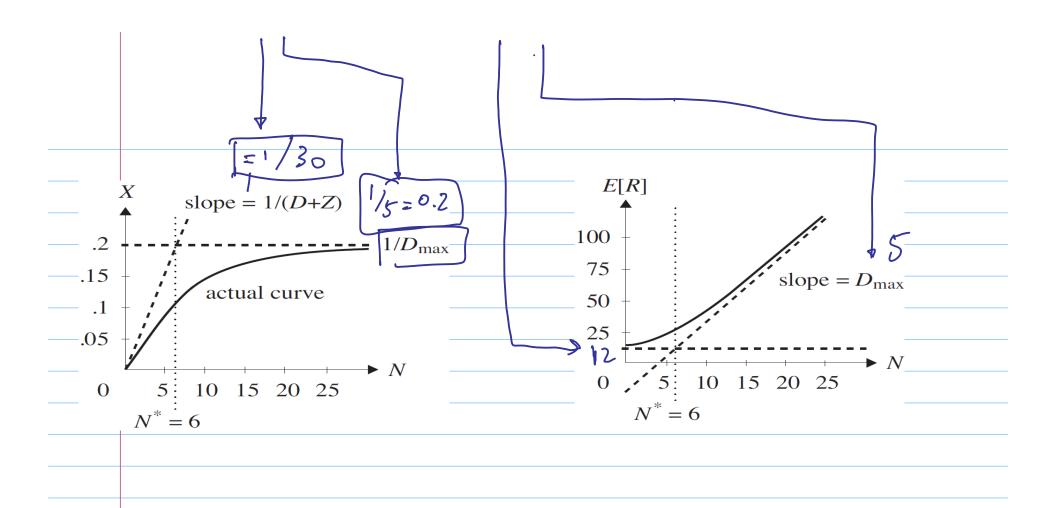
$$X \leq \min\left(\frac{N}{D + \mathbf{E}\left[Z\right]}, \frac{1}{D_{\max}}\right).$$

$$\mathbf{E}\left[R\right] \geq \max\left(D, N \cdot D_{\max} - \mathbf{E}\left[Z\right]\right).$$

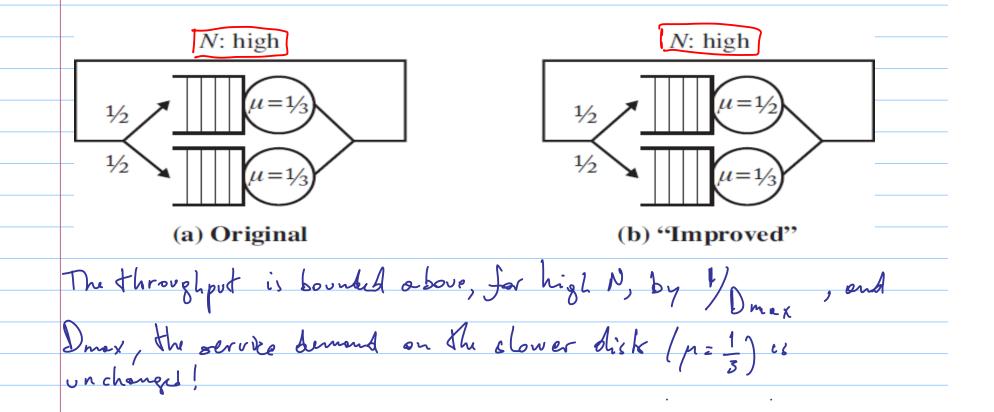
Importantly, the first term in each clause $(\frac{N}{D + \mathbf{E}[Z]})$ or D is an asymptote for small N, and the second term $(\frac{1}{D_{\max}})$ or $N \cdot D_{\max} - \mathbf{E}[Z]$ is an asymptote for large N.

For law N, There is no forcongestion," so the bound is tight. E[R]+E[2] D+E[2] ·

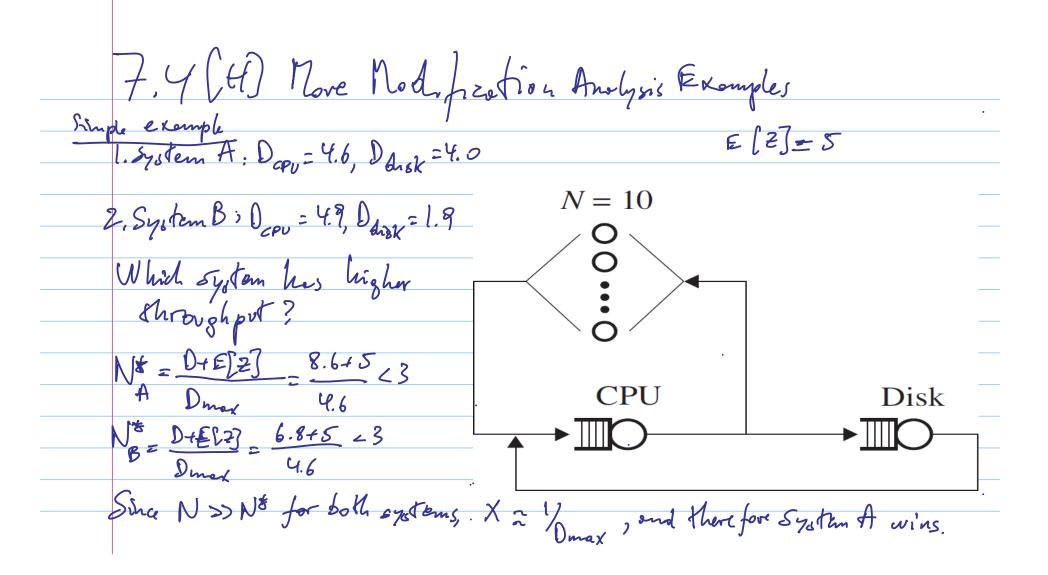
A Simple Example of Bounds E[2]=18 sec E[DCAN] = 540 E[Daiska]= 4sec E[Dolisks]= 3 sec Disk a So, D= 54443 = 12 sec Dmex = 5 (the CPU is the **CPU** Disk b bottleneck Levice) in out Thm. 7.1 ollows us to conclude that Central subsystem [Fix 7.1 [H]] $\times \frac{1}{12+18}$ Cen $\left\{ \frac{N}{12+18}, \frac{1}{5} \right\}, \text{ and } Cen$ $\left\{ \frac{1}{12+18}, \frac{1}{5} \right\}, \text{ and } \frac{1}{1}, \frac{5}{1}, \frac{5}{1}, \frac{5}{1}, \frac{1}{1}, \frac{5}{1}, \frac{1}{1}, \frac{5}{1}, \frac{1}{1}, \frac{5}{1}, \frac{1}{1}, \frac{1}{1},$



7.3 [4] Modification Analysis for Closed Systems



Important Observations Sand E[R] meet at No = D+E[2] · No represents the point beyond which there must be some grevery in the system (E[R]>D). · For fixed N>N*, to increase throughput or lower response time one must reduce D max. Other changes will be hargely - If \(\in (\frac{1}{2}) = 0 \) (both case), \(\mathbb{N}^*\) decreases, i.e., the stormination of \(\text{D} me \times \text{occurs with fower jobs in the system} \)

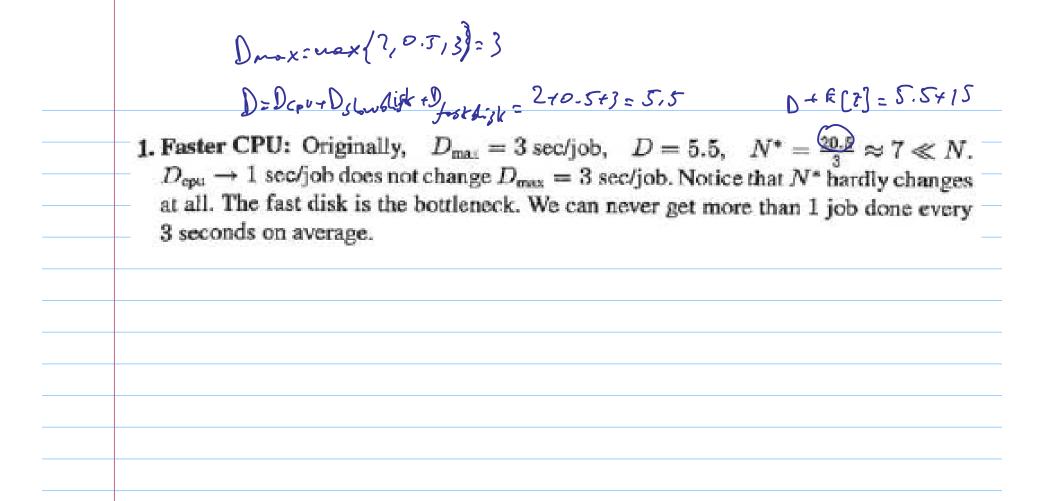


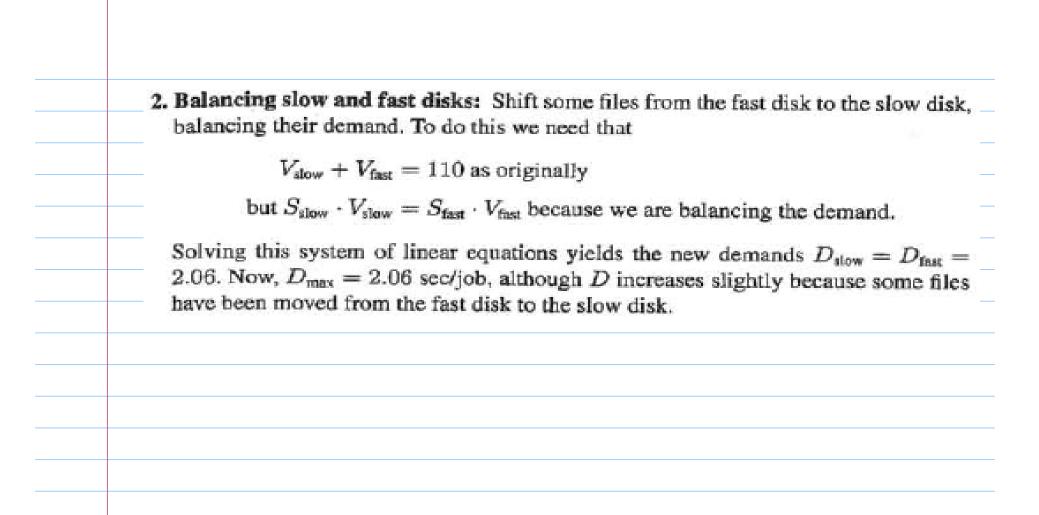
The following measurements were ob	stained for an interactive system2:
• $T = 650$ seconds (the length of	the observation interval)
• $B_{cou} = 400$ seconds	
• $B_{\text{slowdisk}} = 100 \text{ seconds}$	
 B_{fastdisk} = 600 seconds 	
• $C = C_{cpu} = 200 \text{ jobs}$	
• $C_{\text{slowdisk}} = 2,000 \text{ jobs}$	
• $C_{\text{fastdisk}} = 20,000 \text{ jobs}$	
 E [Z] = 15 seconds 	
• $N=20$ users	

nam	nis example, we examine four possible improvements (modifications) – hence the "modification analysis."
	. Faster CPU: Replace the CPU with one that is twice as fast.
2	 Balancing slow and fast disks: Shift some files from the fast disk to the slow disk, balancing their demand.
3	 Second fast disk: Buy a second fast disk to handle half the load of the busic existing fast disk.
4	 Balancing among three disks plus faster CPU: Make all three improvement together: Buy a second fast disk, balance the load across all three disks, and als
	replace the CPU with a faster one.

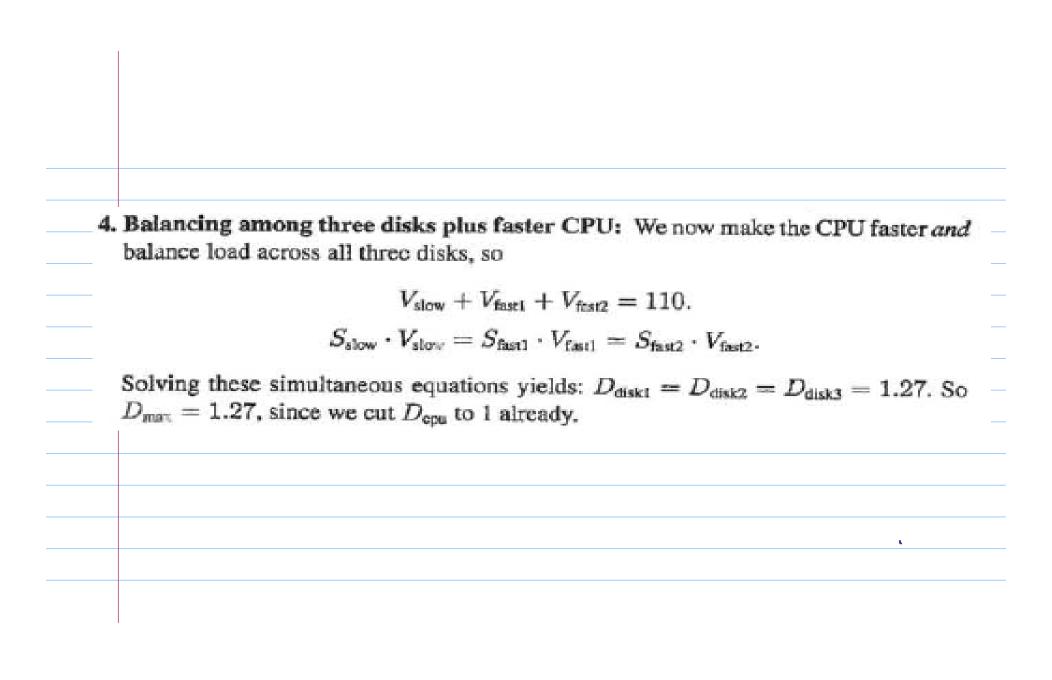


- $D_{\text{cpu}} = B_{\text{cpu}}/C = 400 \text{ sec}/200 \text{ jobs} = 2.0 \text{ sec/job}$
- $D_{\text{slowdisk}} = B_{\text{slowdisk}}/C = 100 \text{ sec}/200 \text{ jobs} = 0.5 \text{ sec/job}$
- $D_{\text{fastdisk}} = B_{\text{fastdisk}}/C = 600 \text{ sec}/200 \text{ jobs } = 3.0 \text{ sec/job}$
- $\mathbf{E}[V_{\text{cpu}}] = C_{\text{cpu}}/C = 200 \text{ visits}/200 \text{ jobs} = 1 \text{ visit/job}$
- $\mathbf{E}\left[V_{\mathrm{slowdisk}}
 ight] = C_{\mathrm{slowdisk}}/C = 2{,}000\ \mathrm{visits/200\ job} = 10\ \mathrm{visits/job}$
- $\mathbf{E}\left[V_{\mathsf{fastdisk}}\right] = C_{\mathsf{fastdisk}}/C = 20,000 \text{ visits}/200 \text{ job} = 100 \text{ visits/job}$
- $\mathbf{E}[S_{\text{cpu}}] = B_{\text{cpu}}/C_{\text{cpu}} = 400 \text{ sec}/200 \text{ visits} = 2.0 \text{ sec/visit}$
- $\mathbf{E}[S_{\text{slowdisk}}] = B_{\text{slowdisk}}/C_{\text{slowdisk}} = 100 \text{ sec}/2,000 \text{ visits} = .05 \text{ sec/visit}$
- $\mathbf{E}[S_{\text{fastdisk}}] = B_{\text{fastdisk}}/C_{\text{fastdisk}} = 600 \text{ sec}/20,000 \text{ visits} = .03 \text{ sec/visit}$





3. Second fast disk: We keep $D_{\text{flow}} = 0.5$, the same as before. However, we buy second fast disk to handle half the load of the original fast disk. So now
$D_{ m fast1} = D_{ m fast2} = 1.5~{ m sec/job}.$
Thus our new $D_{\rm max}$ is 2.0 sec/job (the CPU becomes the bottleneck).
•



A graph of the results is shown in Figure 7.5. Assuming N is not too small, we conclude the following:

- Change 1 is insignificant.
- Changes 2 and 3 are about the same, which is interesting because change 2 was achieved without any hardware expense.
- Change 4 yields the most dramatic improvement.

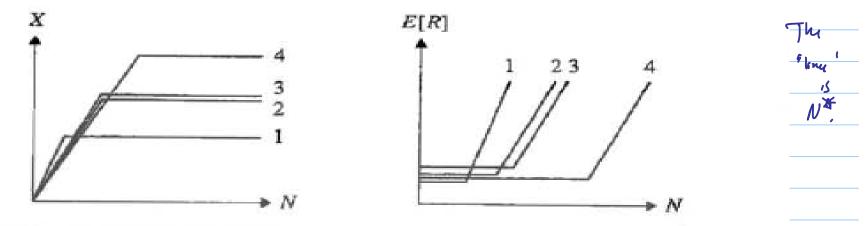


Figure 7.5. Throughput and response time versus N, showing the effects of four possible improvements from the harder example, where the improvements are labeled 1, 2, 3, and 4.

Why does modification analysis und apply to open systems?